

$$y = a \cdot \cos(x) + d$$

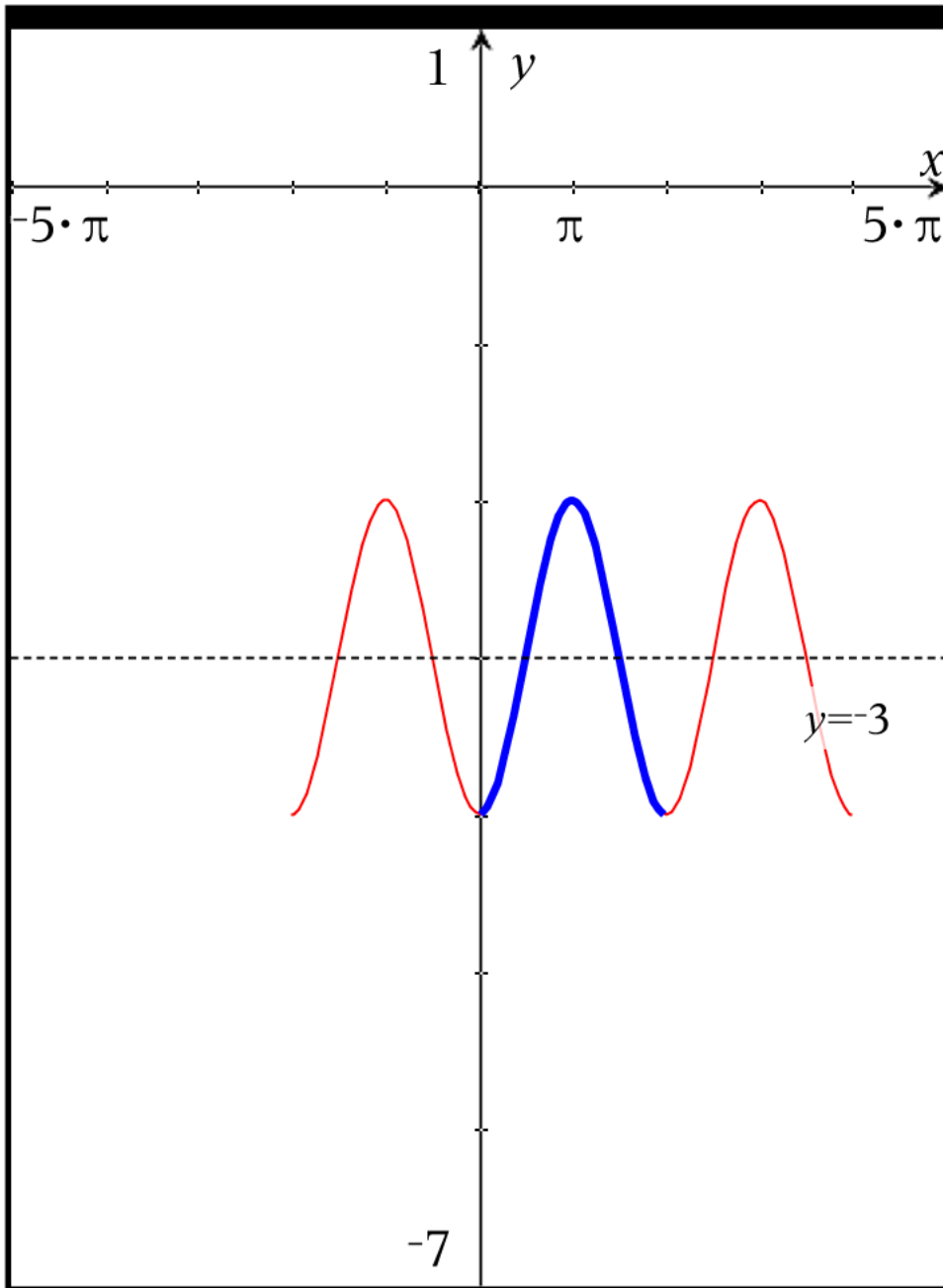
ONE PERIOD = $[0, 2 \cdot \pi)$

Range $[-3, 1]$

This graph is a VERTICAL STRETCH
(Range doubled)

This graph is a VERTICAL SHIFT DOWN 2

This means ONE VERSION of this graph is
 $y = 2\cos(x) - 2$



$$y = a \cdot \cos(x) + d$$

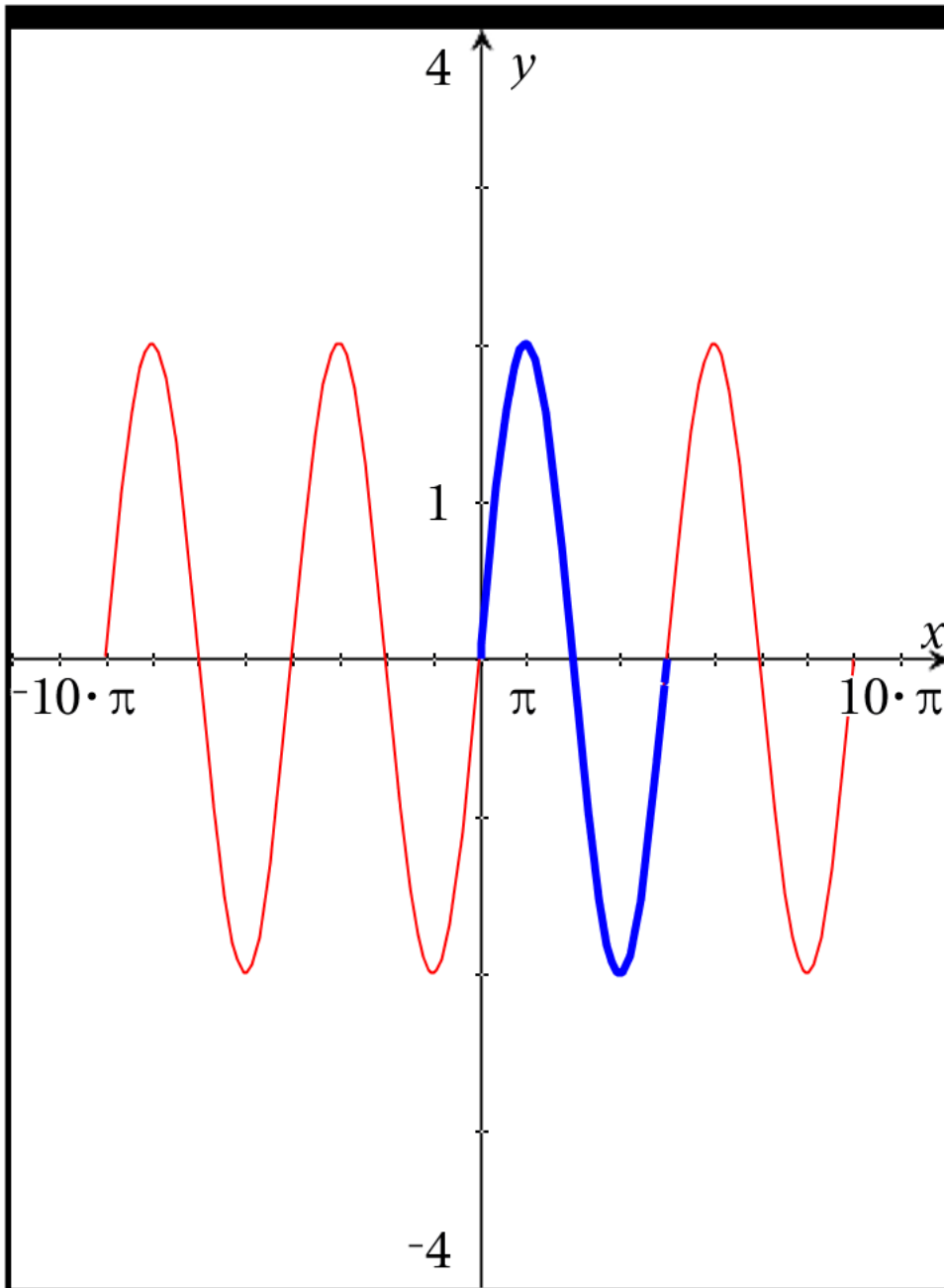
ONE PERIOD = $[0, 2 \cdot \pi)$

Range $[-4, -2]$

This graph is a VERTICAL REFLECTION over $y = -3$

This graph is a VERTICAL SHIFT DOWN 3 units

This means ONE VERSION of this graph is $y = -1 \cos(x) - 3$



$$y = a \cdot \sin(bx + c) = a \cdot \sin\left(b\left(x + \frac{c}{b}\right)\right)$$

ONE PERIOD = $[0, 4 \cdot \pi)$

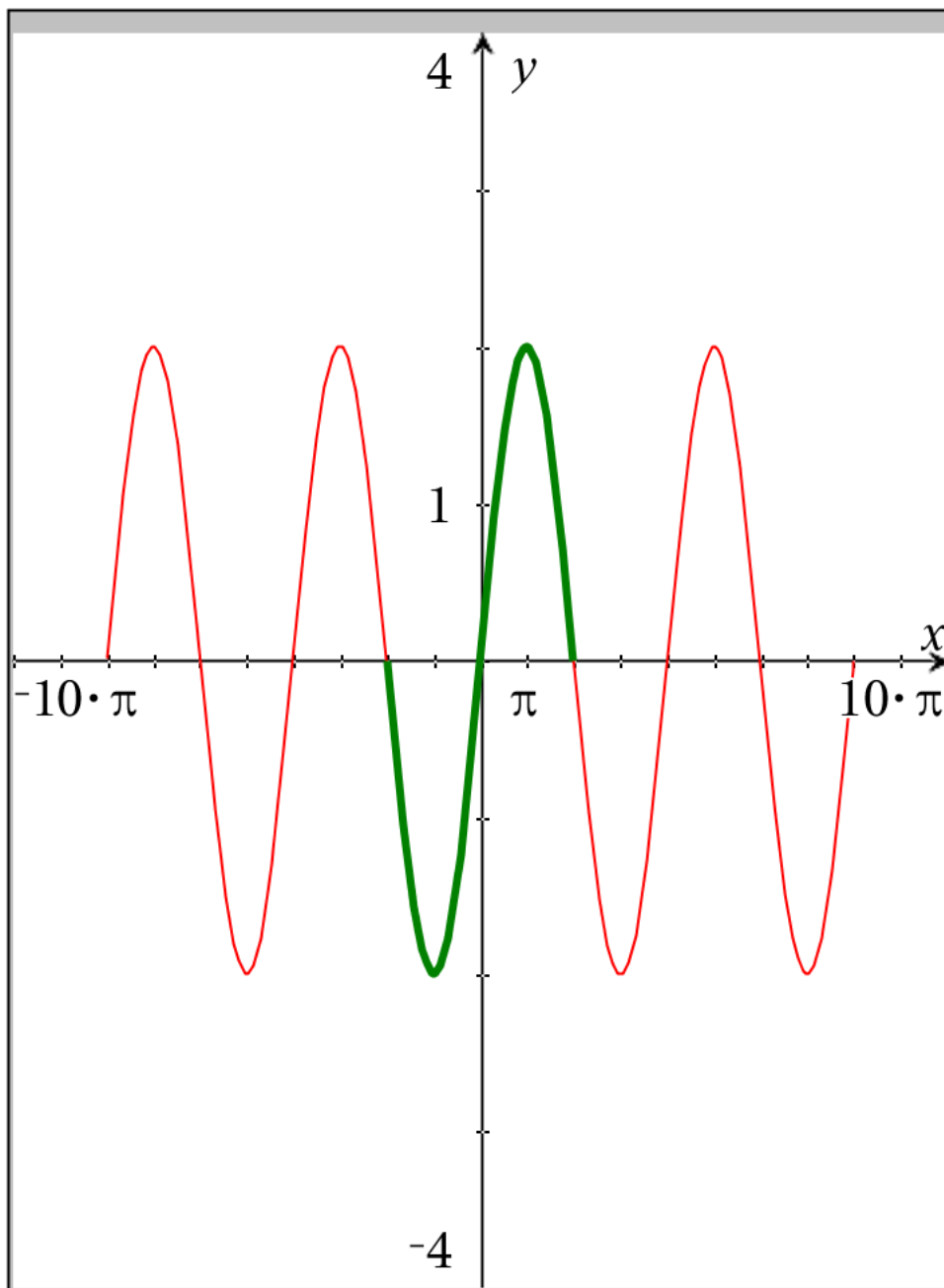
Range $[-2, 2]$

This graph is a VERTICAL STRETCH
(range doubled)

This graph is a HORIZONTAL STRETCH
(period doubled)

This means ONE VERSION of this graph is

$$y = 2\sin\left(\frac{1}{2}x\right)$$



$$y = a \cdot \sin(bx + c) = a \cdot \sin\left(b\left(x + \frac{c}{b}\right)\right)$$

ONE PERIOD = $[-2 \cdot \pi, 2 \cdot \pi)$

Range $[-2, 2]$

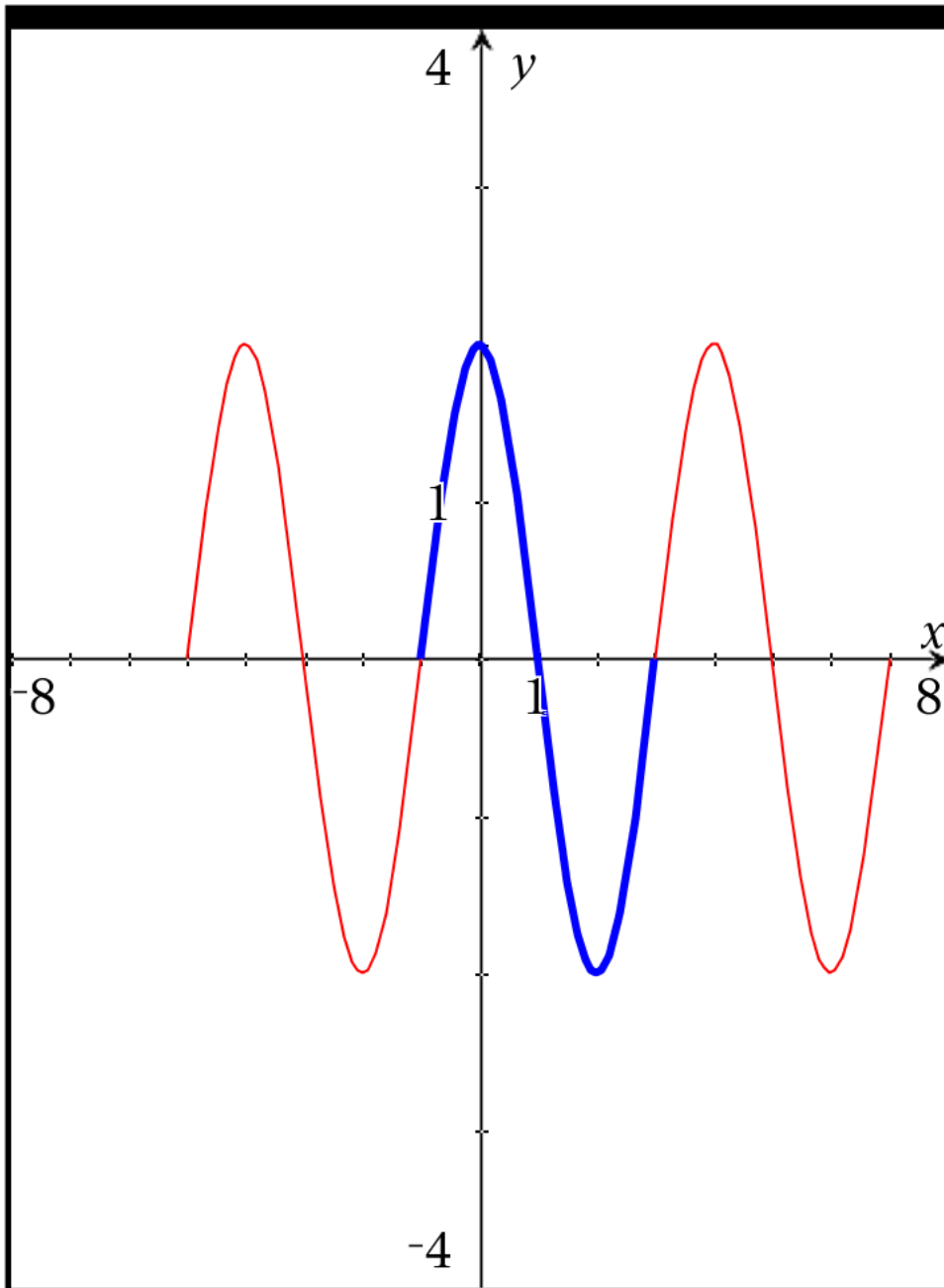
This graph is a VERTICAL STRETCH
(range doubled)

This graph is a VERTICAL Reflection

This graph is a HORIZONTAL SHIFT LEFT $2 \cdot \pi$

This means ANOTHER VERSION of this graph is

$$y = -2 \cdot \sin\left(\frac{1}{2} \cdot (x + 2 \cdot \pi)\right) = -2 \cdot \sin\left(\frac{1}{2} \cdot x + \pi\right)$$



$$y = a \cdot \sin(bx + c) = a \cdot \sin\left(b\left(x + \frac{c}{b}\right)\right)$$

ONE PERIOD = $[-1, 3)$

Range $[-2, 2]$

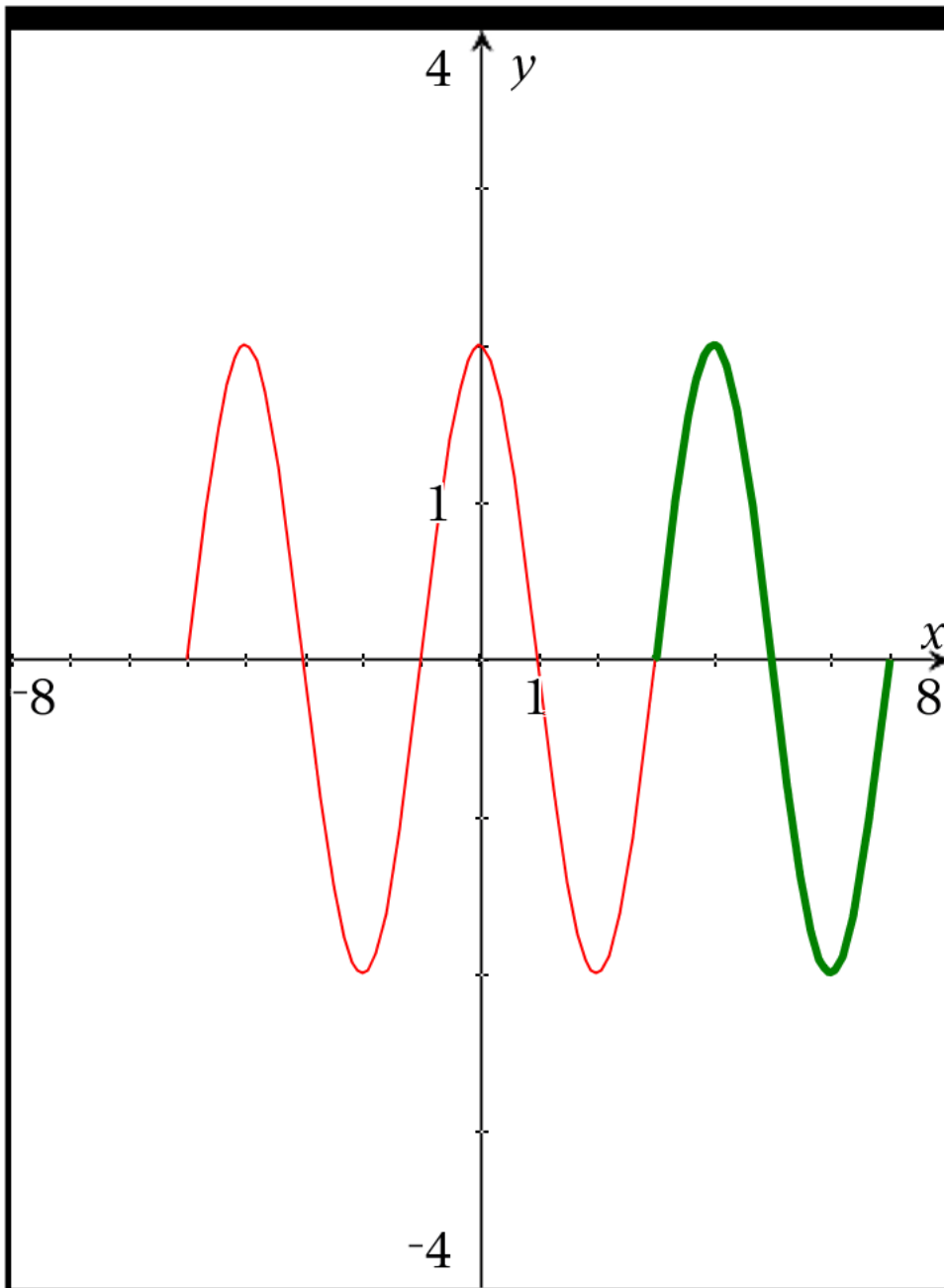
This graph is a VERTICAL STRETCH
(range doubled)

This graph is a HORIZONTAL COMPRESSION
(period is NOW 4 units $< 2 \cdot \pi$ units)

This graph is a HORIZONTAL SHIFT LEFT 1 units

This means ONE VERSION of this graph is

$$y = 2 \cdot \sin\left(\frac{\pi}{2} \cdot (x+1)\right) = 2 \cdot \sin\left(\frac{\pi}{2} \cdot x + \frac{\pi}{2}\right)$$



$$y = a \cdot \sin(bx + c) = a \cdot \sin\left(b\left(x + \frac{c}{b}\right)\right)$$

ONE PERIOD = $[-1, 3)$

Range $[-2, 2]$

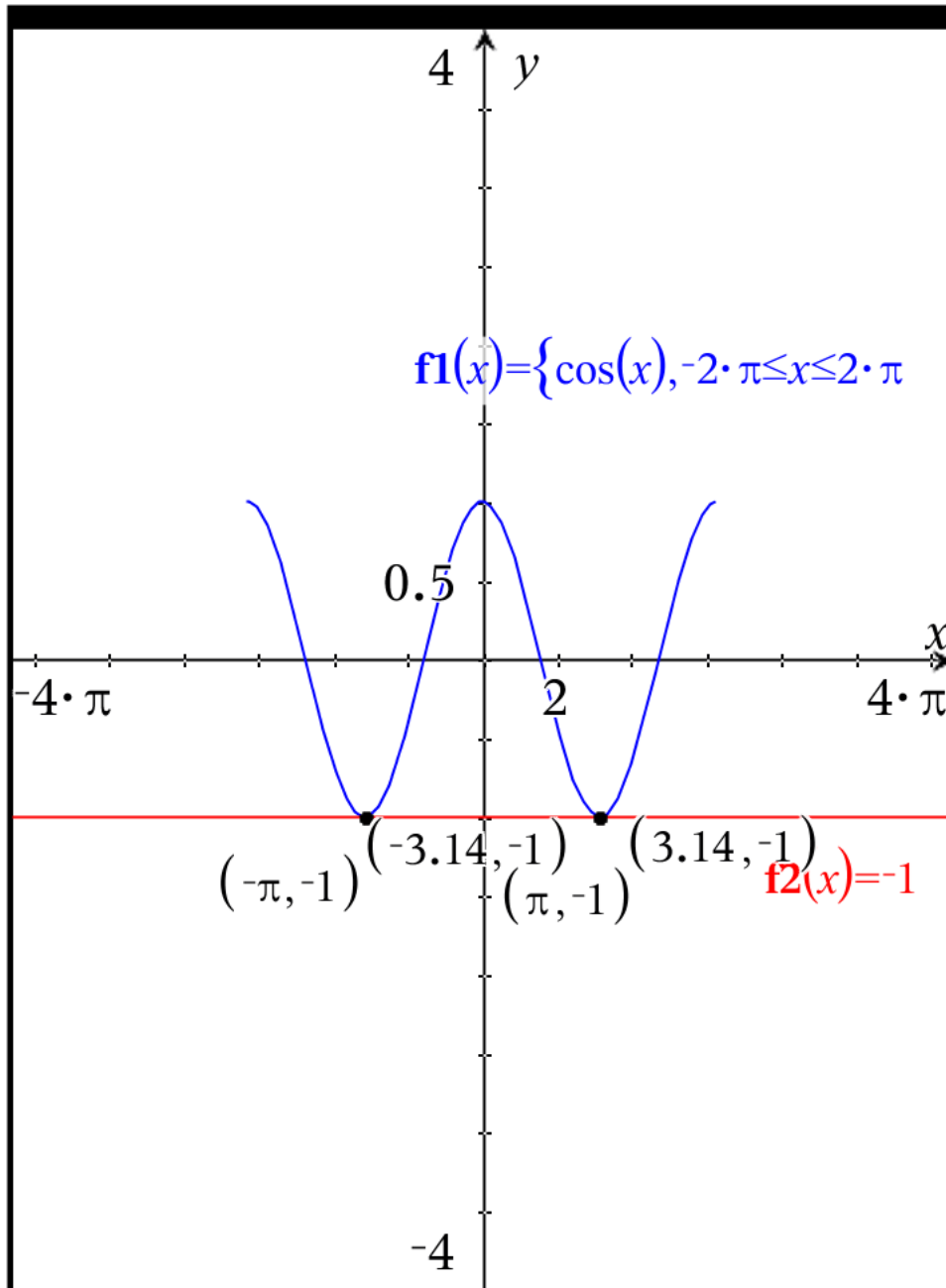
This graph is a VERTICAL STRETCH
(range doubled)

This graph is a HORIZONTAL COMPRESSION
(period is NOW 4 units $< 2 \cdot \pi$ units)

This graph is a HORIZONTAL SHIFT RIGHT 3 units

This means ANOTHER VERSION of this graph is

$$y = 2 \cdot \sin\left(\frac{\pi}{2} \cdot (x - 3)\right) = 2 \cdot \sin\left(\frac{\pi}{2} \cdot x - \frac{3\pi}{2}\right)$$



This question is asking us to solve the trigonometric system over $[-2\pi, 2\pi]$

$$y = \cos(x)$$

$$y = -1$$

(you really don't need a graphing calculator to do this, you should not need any calculator if you know your chart and reference angles)

$$-1 = \cos(x)$$

$$\cos^{-1}(-1) = x$$

$\pi = x$ (remember to switch your calculator to radian mode)

NOW we can reference back to $x = -\pi$

This question is asking us to solve the trigonometric system over $[-2\pi, 2\pi]$

$$y = \sin(x)$$

$$y = \frac{\sqrt{3}}{2}$$

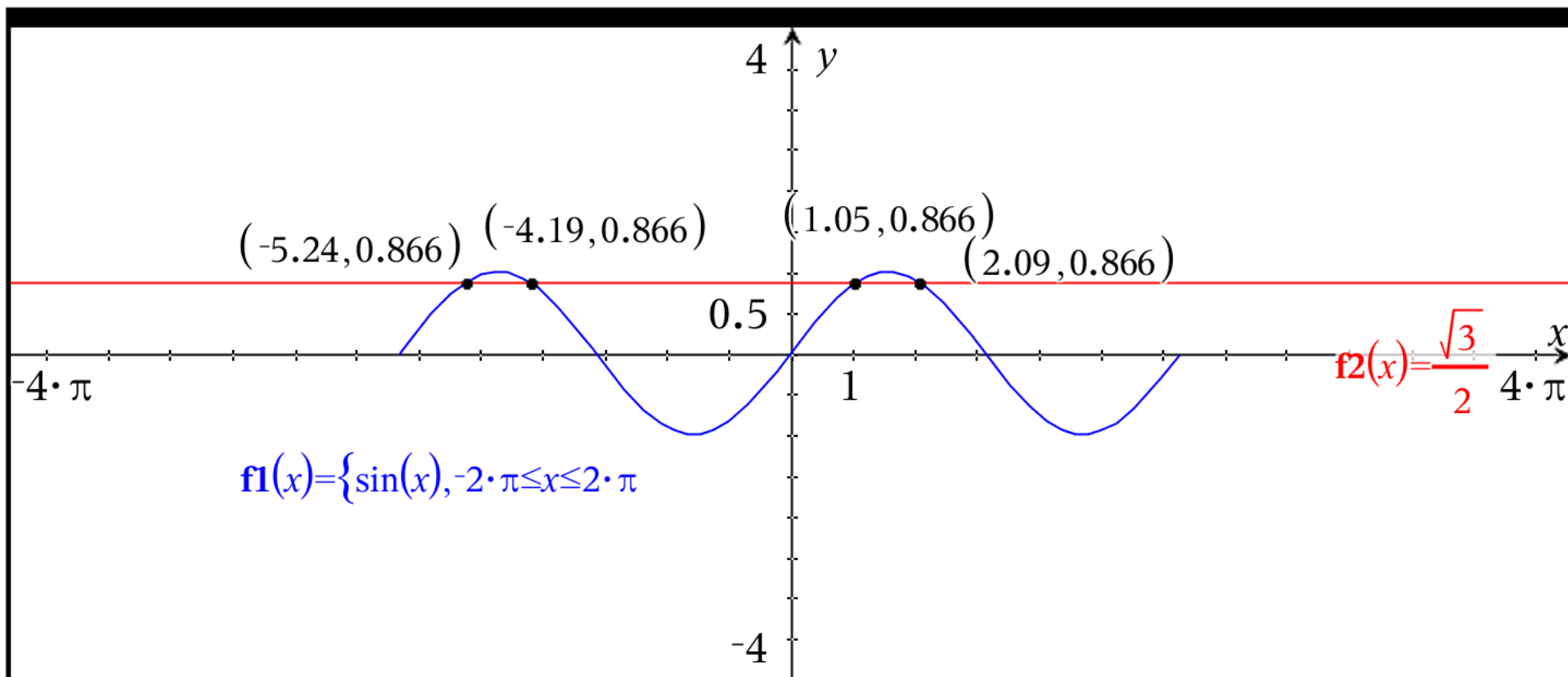
(you really don't need a graphing calculator to do this, you should not need any calculator if you know your chart and reference angles)

$$\frac{\sqrt{3}}{2} = \sin(x)$$

$$\sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = x$$

$$\frac{\pi}{3} = x \quad (\text{remember to switch your calculator to radian mode})$$

NOW we can reference to $x = \frac{2\pi}{3}$, $x = \frac{-4 \cdot \pi}{3}$, and $x = \frac{-5 \cdot \pi}{3}$



Note $\frac{\sqrt{3}}{2} \approx 0.866025$ Note: $\frac{\pi}{3} \approx 1.0472$ Note: $\frac{2\pi}{3} \approx 2.0944$

Note: $\frac{-4\pi}{3} \approx -4.18879$ Note: $\frac{5\pi}{3} \approx 5.23599$

