

Problem 1

	A	B	C	D	E	F	G
=							
1	seq_num	value	difference	diff_diff			
2	1	-125	-20	-5			
3	2	-145	-25	-5			
4	3	-170	-30	-5			
5	4	-200	-35				
6	5	-235					
7							
8							
9							
10							
11							

A1 seq\_num

$$\{-125, -145, -170, -200, -235\}$$

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to add  $-20$  to its first term and then only and then after that only add  $-5$  to each successive term

$$a_1 = -125 \quad (\text{this is always just stated in a recursive sequence})$$

$$a_2 = -145 = -125 + [-20 + 0(-5)]$$

$$a_3 = -170 = -145 + [-20 + 1(-5)]$$

$$a_4 = -200 = -170 + [-20 + 2(-5)]$$

$$a_5 = -235 = -200 + [-20 + 3(-5)]$$

$a_1 = -125$  (this is always just stated in a recursive sequence)

**notice that the highlighted counters are off by 2**

$$a_2 = -145 = -125 + [-20 + 0(-5)]$$

$$a_3 = -170 = -145 + [-20 + 1(-5)]$$

$$a_4 = -200 = -170 + [-20 + 2(-5)]$$

$$a_5 = -235 = -200 + [-20 + 3(-5)]$$

$a_1 = -125$  (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number,  $n$ .

$$a_2 = -145 = -125 + [-20 + (n-2)(-5)]$$

$$a_3 = -170 = -145 + [-20 + (n-2)(-5)]$$

$$a_4 = -200 = -170 + [-20 + (n-2)(-5)]$$

$$a_5 = -235 = -200 + [-20 + (n-2)(-5)]$$

$a_1 = -125$  (this is always just stated in a recursive sequence)

**Use the pattern to find the next two terms**

$$a_2 = -145 = -125 + [-20 + (2-2)(-5)]$$

$$a_3 = -170 = -145 + [-20 + (3-2)(-5)]$$

$$a_4 = -200 = -170 + [-20 + (4-2)(-5)]$$

$$a_5 = -235 = -200 + [-20 + (5-2)(-5)]$$

$$a_6 = -275 = -235 + [-20 + (6-2)(-5)]$$

$$a_7 = -320 = -275 + [-20 + (7-2)(-5)]$$

So now we can write a rule for the sequence  $\{-125, -145, -170, -200, -235\}$

$$a_1 = -125$$

$$a_n = a_{n-1} + [-20 + (n-2)(-5)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} + -5 \cdot n - 10$$

Problem 2

	A	B	C	D	E	F	G
=							
1	seq_num	value	difference	diff_diff			
2	1	16	33	6			
3	2	49	39	6			
4	3	88	45	6			
5	4	133	51				
6	5	184					
7							
8							
9							
10							
11							

A1 seq\_num

$\{16, 49, 88, 133, 184\}$ 

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to add 33 to its first term and then only and then after that only add 6 to each successive term

$a_1 = 16$  (this is always just stated in a recursive sequence)

$$a_2 = 49 = 16 + [33 + 0(6)]$$

$$a_3 = 88 = 49 + [33 + 1(6)]$$

$$a_4 = 133 = 88 + [33 + 2(6)]$$

$$a_5 = 184 = 133 + [33 + 3(6)]$$



$a_1 = 16$  (this is always just stated in a recursive sequence)

**notice that the highlighted counters are off by 2**

$$a_2 = 49 = 16 + [33 + 0(6)]$$

$$a_3 = 88 = 49 + [33 + 1(6)]$$

$$a_4 = 133 = 88 + [33 + 2(6)]$$

$$a_5 = 184 = 133 + [33 + 3(6)]$$

$a_1 = 16$  (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number,  $n$ .

$$a_2 = 49 = 16 + [33 + (n-2)(6)]$$

$$a_3 = 88 = 49 + [33 + (n-2)(6)]$$

$$a_4 = 133 = 88 + [33 + (n-2)(6)]$$

$$a_5 = 184 = 133 + [33 + (n-2)(6)]$$

$a_1 = 16$  (this is always just stated in a recursive sequence)

**Use the pattern to find the next two terms**

$$a_2 = 49 = 16 + [33 + (2-2)(6)]$$

$$a_3 = 88 = 49 + [33 + (3-2)(6)]$$

$$a_4 = 133 = 88 + [33 + (4-2)(6)]$$

$$a_5 = 184 = 133 + [33 + (5-2)(6)]$$

$$a_6 = 241 = 184 + [33 + (6-2)(6)]$$

$$a_7 = 304 = 241 + [33 + (7-2)(6)]$$

So now we can write a rule for the sequence  $\{16, 49, 88, 133, 184\}$

$$a_1 = 16$$

$$a_n = a_{n-1} + [33 + (n-2)(6)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} + 6 \cdot n + 21$$

Problem 3

	A	B	C	D	E	F	G
=							
1	seq_num	value	ratio	diff_ratio			
2	1	4	55	5			
3	2	220	60	5			
4	3	13200	65	5			
5	4	858000	70				
6	5	60060000					
7							
8							
9							
10							
11							

A1 seq\_num

$\{4, 220, 13200, 858000, 60060000\}$

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to multiply by 55 to its first term and then only and then after that multiply by 5 more than the previous term to each successive term

$a_1 = 4$  (this is always just stated in a recursive sequence)

$$a_2 = 220 = 4 [55 + 0(5)]$$

$$a_3 = 13200 = 220 [55 + 1(5)]$$

$$a_4 = 858000 = 13200 [55 + 2(5)]$$

$$a_5 = 60060000 = 858000 [55 + 3(5)]$$

$a_1 = 4$  (this is always just stated in a recursive sequence)

**notice that the highlighted counters are off by 2**

$$a_2 = 220 = 4[55 + 0(5)]$$

$$a_3 = 13200 = 220[55 + 1(5)]$$

$$a_4 = 858000 = 13200[55 + 2(5)]$$

$$a_5 = 60060000 = 858000[55 + 3(5)]$$

$a_1 = 4$  (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number,  $n$ .

$$a_2 = 220 = 4 [55 + (n-2)(5)]$$

$$a_3 = 13200 = 220 [55 + (n-2)(5)]$$

$$a_4 = 858000 = 13200 [55 + (n-2)(5)]$$

$$a_5 = 60060000 = 858000 [55 + (n-2)(5)]$$



$a_1 = 4$  (this is always just stated in a recursive sequence)

**Use the pattern to find the next two terms**

$$a_2 = 220 = 4 + [55 + (2-2)(5)]$$

$$a_3 = 13200 = 220 + [55 + (3-2)(5)]$$

$$a_4 = 858000 = 13200 + [55 + (4-2)(5)]$$

$$a_5 = 60060000 = 858000 + [55 + (5-2)(5)]$$

$$a_6 = 4504500000 = 60060000 + [55 + (6-2)(5)]$$

$$a_7 = 360360000000 = 4504500000 + [55 + (7-2)(5)]$$

So now we can write a rule for the sequence  $\{4, 220, 13200, 858000, 60060000\}$

$$a_1 = 4$$

$$a_n = a_{n-1} [55 + (n-2)(5)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} [5 \cdot n + 45]$$