

Problem 1

	A	B	C	D	E	F	G
=							
1	seq_num	value	difference	diff_diff			
2	1	-165	-100	-15			
3	2	-265	-115	-15			
4	3	-380	-130	-15			
5	4	-510	-145				
6	5	-655					
7							
8							
9							
10							
11							

A1 seq_num

$$\{-165, -265, -380, -510, -655\}$$

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to add -100 to its first term and then only and then after that only add -15 to each successive term

$$a_1 = -165 \quad (\text{this is always just stated in a recursive sequence})$$

$$a_2 = -265 = -165 + [-100 + 0(-15)]$$

$$a_3 = -380 = -265 + [-100 + 1(-15)]$$

$$a_4 = -510 = -380 + [-100 + 2(-15)]$$

$$a_5 = -655 = -510 + [-100 + 3(-15)]$$

$a_1 = -165$ (this is always just stated in a recursive sequence)

notice that the highlighted counters are off by 2

$$a_2 = -265 = -165 + [-100 + 0(-15)]$$

$$a_3 = -380 = -265 + [-100 + 1(-15)]$$

$$a_4 = -510 = -380 + [-100 + 2(-15)]$$

$$a_5 = -655 = -510 + [-100 + 3(-15)]$$

$a_1 = -165$ (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number, n .

$$a_2 = -265 = -165 + [-100 + (n-2)(-15)]$$

$$a_3 = -380 = -265 + [-100 + (n-2)(-15)]$$

$$a_4 = -510 = -380 + [-100 + (n-2)(-15)]$$

$$a_5 = -655 = -510 + [-100 + (n-2)(-15)]$$

$a_1 = -165$ (this is always just stated in a recursive sequence)

Use the pattern to find the next two terms

$$a_2 = -265 = -165 + [-100 + (2-2)(-15)]$$

$$a_3 = -380 = -265 + [-100 + (3-2)(-15)]$$

$$a_4 = -510 = -380 + [-100 + (4-2)(-15)]$$

$$a_5 = -655 = -510 + [-100 + (5-2)(-15)]$$

$$a_6 = -815 = -655 + [-100 + (6-2)(-15)]$$

$$a_7 = -990 = -815 + [-100 + (7-2)(-15)]$$

So now we can write a rule for the sequence $\{-165, -265, -380, -510, -655\}$

$$a_1 = -165$$

$$a_n = a_{n-1} + [-100 + (n-2)(-15)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} + -15 \cdot n - 70$$

Problem 2

	A	B	C	D	E	F	G
=							
1	seq_num	value	difference	diff_diff			
2	1	27	88	16			
3	2	115	104	16			
4	3	219	120	16			
5	4	339	136				
6	5	475					
7							
8							
9							
10							
11							

A1 seq_num

$\{27, 115, 219, 339, 475\}$

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to add 88 to its first term and then only and then after that only add 16 to each successive term

$a_1 = 27$ (this is always just stated in a recursive sequence)

$$a_2 = 115 = 27 + [88 + 0(16)]$$

$$a_3 = 219 = 115 + [88 + 1(16)]$$

$$a_4 = 339 = 219 + [88 + 2(16)]$$

$$a_5 = 475 = 339 + [88 + 3(16)]$$

$a_1 = 27$ (this is always just stated in a recursive sequence)

notice that the highlighted counters are off by 2

$$a_2 = 115 = 27 + [88 + 0(16)]$$

$$a_3 = 219 = 115 + [88 + 1(16)]$$

$$a_4 = 339 = 219 + [88 + 2(16)]$$

$$a_5 = 475 = 339 + [88 + 3(16)]$$

$a_1 = 27$ (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number, n .

$$a_2 = 115 = 27 + [88 + (n-2)(16)]$$

$$a_3 = 219 = 115 + [88 + (n-2)(16)]$$

$$a_4 = 339 = 219 + [88 + (n-2)(16)]$$

$$a_5 = 475 = 339 + [88 + (n-2)(16)]$$

$a_1 = 27$ (this is always just stated in a recursive sequence)

Use the pattern to find the next two terms

$$a_2 = 115 = 27 + [88 + (2-2)(16)]$$

$$a_3 = 219 = 115 + [88 + (3-2)(16)]$$

$$a_4 = 339 = 219 + [88 + (4-2)(16)]$$

$$a_5 = 475 = 339 + [88 + (5-2)(16)]$$

$$a_6 = 627 = 475 + [88 + (6-2)(16)]$$

$$a_7 = 795 = 627 + [88 + (7-2)(16)]$$

So now we can write a rule for the sequence $\{27, 115, 219, 339, 475\}$

$$a_1 = 27$$

$$a_n = a_{n-1} + [88 + (n-2)(16)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} + 16 \cdot n + 56$$

Problem 3

	A	B	C	D	E	F	G
=							
1	seq_num	value	ratio	diff_ratio			
2	1	8	77	7			
3	2	616	84	7			
4	3	51744	91	7			
5	4	4708704	98				
6	5	461452992					
7							
8							
9							
10							
11							

A1 seq_num

$\{8,616,51744,4708704,461452992\}$

this sequence is NOT arithmetic nor geometric

this sequence can be written as a recursive pattern

The pattern changes after the second term to an arithmetic pattern

THE PATTERN

So we need to get a sequence to multiply by 77 to its first term and then only and then after that multiply by 7 more than the previous term to each successive term

$a_1 = 8$ (this is always just stated in a recursive sequence)

$$a_2 = 616 = 8 [77 + 0(7)]$$

$$a_3 = 51744 = 616 [77 + 1(7)]$$

$$a_4 = 4708704 = 51744 [77 + 2(7)]$$

$$a_5 = 461452992 = 4708704 [77 + 3(7)]$$

$a_1 = 8$ (this is always just stated in a recursive sequence)

notice that the highlighted counters are off by 2

$$a_2 = 616 = 8 [77 + 0(7)]$$

$$a_3 = 51744 = 616 [77 + 1(7)]$$

$$a_4 = 4708704 = 51744 [77 + 2(7)]$$

$$a_5 = 461452992 = 4708704 [77 + 3(7)]$$

$a_1 = 8$ (this is always just stated in a recursive sequence)

Since the highlighted counters are off by 2,

lets make that adjustment by subtracting 2 from sequence number, n .

$$a_2 = 616 = 8 [77 + (n-2)(7)]$$

$$a_3 = 51744 = 616 [77 + (n-2)(7)]$$

$$a_4 = 4708704 = 51744 [77 + (n-2)(7)]$$

$$a_5 = 461452992 = 4708704 [77 + (n-2)(7)]$$

$a_1 = 8$ (this is always just stated in a recursive sequence)

Use the pattern to find the next two terms

$$a_2 = 616 = 8 + [77 + (2-2)(7)]$$

$$a_3 = 51744 = 616 + [77 + (3-2)(7)]$$

$$a_4 = 4708704 = 51744 + [77 + (4-2)(7)]$$

$$a_5 = 461452992 = 4708704 + [77 + (5-2)(7)]$$

$$a_6 = 48452564160 = 461452992 + [77 + (6-2)(7)]$$

$$a_7 = 5426687185920 = 48452564160 + [77 + (7-2)(7)]$$

So now we can write a rule for the sequence $\{8, 616, 51744, 4708704, 461452992\}$

$$a_1 = 8$$

$$a_n = a_{n-1} [77 + (n-2)(7)]$$

Now the second part of the rule has an EXPLICIT formula that all versions of this rule must eventually become

$$a_n = a_{n-1} [7 \cdot n + 63]$$