

Problem 1

A		S Method $a_n = 275 + (n-1)(-6.5)$
=		
1	a_1	$a_{1000} = 275 + (1000-1)(-6.5)$
2	d	$= -6218.5$
3	n_1	$S_{1000} = (1000/2)[275 + -6218.5]$
4	n_2	$= -2971750.$
5		$= -2.97175E6$ (scientific notation)
6		<b>infinite sum</b> $-\infty$
7		
8		
9		
10		
11		
		$\sum_{n=1}^{1000} 275 + (n-1)(-6.5) = -2.97175E6$
A1 a_1		

Problem 2

A	B	S Method $a_n = 1826 + (n-1)(2.4)$
=		
1	a_1	$a_{85} = 1826 + (85-1)(2.4)$
2	d	$= 2027.6$
3	n_1	
4	n_2	$S_{85} = (85/2)[1826 + 2027.6]$
5		$= 163778.$
6		
7		
8		<b>infinite sum</b> $\infty$
9		
10		
11		
		$\sum_{n=1}^{85} 1826 + (n-1)(2.4) = 163778.$
A1 a_1		

### Problem 3

A	B
=	
1 a_1	
2	
3 n_1	
4 n_2	
5	
6	
7	
8	
9	
10	
11	
AI a_1	

$$S_{26} = \frac{1 - \left(\frac{7}{13}\right)^{26}}{1 - \frac{7}{13}} = \frac{611555472038588526737635402400}{7056410014866816666030739693} \approx 86.6667$$

$$S_9 = \frac{1 - \left(\frac{7}{13}\right)^9}{1 - \frac{7}{13}} = \frac{70427638440}{815730721} \approx 86.3369$$

$$S_{26} - S_9 = \frac{2327107312779470308854457880}{7056410014866816666030739693} \approx 0.3298$$

$$n_{-1} \sum_{n=10}^{26} 40 \left(\frac{7}{13}\right)^{n-1} = \frac{2327107312779470308854457880}{7056410014866816666030739693} \approx 0.3298$$

### Problem 4

A	B
=	
1 a_1	
2 d	
3 n_1	
4 n_2	
5	
6	
7	
8	
9	
10	
11	
AI a_1	

S Method  $a_n = 472 + (n-1)(-3.2)$

$a_{58} = 472 + (58-1)(-3.2) = 289.6$

$S_{58} = (58/2)[472 + 289.6] = 22086.4$

$a_{28} = 472 + (28-1)(-3.2) = 385.6$

$S_{28} = (28/2)[472 + 385.6] = 12006.4$

$S_{58} - S_{28} = 22086.4 - 12006.4 = 10080.$

Infinite Sum =  $-\infty$

$$\sum_{n=29}^{58} 472 + (n-1)(-3.2) = 10080.$$

Problem 5

A	B
=	
1	a_1
2	d
3	n_1
4	n_2
5	
6	
7	
8	
9	
10	
11	
A1	a_1

S Method  $a_n = 8400 + (n-1)(24)$

$a_{17} = 8400 + (17-1)(24)$

$= 8784$

$S_{17} = (17/2)[8400 + 8784]$

$= 146064$

**infinite sum**  $\infty$

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$$\sum_{n=1}^{17} 8400 + (n-1)(24) = 146064$$

Problem 6

A	B
=	
1	a_1
2	r
3	n_1
4	n_2
5	
6	
7	
8	
9	
10	
11	
A1	a_1

$a_n = 1400 \left(\frac{8}{7}\right)^{n-1}$

$S_9 = \frac{1 - \left(\frac{8}{7}\right)^9}{1 - \frac{8}{7}} = \frac{18772824200}{823543} \approx 22795.1961$

$\sum_{n=1}^9 1400 \left(\frac{8}{7}\right)^{n-1} = \frac{18772824200}{823543} \approx 22795.1961$

*infinite sum*  $+\infty$

Problem 7

A	B
=	
1 a_1	
2	
3 n_1	
4 n_2	
5	
6	
7	
8	
9	
10	
11	
A1 a_1	

$$a_n = 960 \left( \frac{-8}{15} \right)^{n-1}$$

$$S_6 = \frac{1 - \left( \frac{-8}{15} \right)^6}{1 - \frac{-8}{15}} = \frac{30966208}{50625} \approx 611.6782$$

$$\sum_{n=1}^6 960 \left( \frac{-8}{15} \right)^{n-1} = \frac{30966208}{50625} \approx 611.6782$$

infinite sum  $\frac{14400}{23} \approx 626.086956522$

Problem 8

A	B	C	D	E	F	G	H
=							
1 a_1		98 differenc...		15 ratio		113/98	
A1 a_1							

{98,113,143}

This is a recursive pattern The difference in 113 and 98 is 15  
The difference in 143 and 113 is 30

So a pattern for the change can be written as: Add 15  
Add 15 more than the last time to each term

a\_1 = 98  
a\_n = a\_{n-1} + (15 + (n-2)(15))

a\_1 = 98  
a\_n = a\_{n-1} + (15 · n + 15)

This is a "fancier" version a\_1 = 98 a\_n = 98 +  $\sum_{k=1}^{n-1} (15 + (k-1)(15))$

Problem 9

# TYPHO

Problem 10

A	B	C	D	E	F	G	H
=							
1 a_1	24300000	differenc...	-186300...	ratio		7/30	

AI a\_1

{ 24300000, 5670000, 1323000 }

This is a geometric pattern The ratio is 5670000 divided by 24300000 is  $\frac{7}{30}$

The ratio is 1323000 divided by 5670000 is  $\frac{7}{30}$

$a_1 = 24300000$   $r = \frac{7}{30}$   $a_n = 24300000 \left(\frac{7}{30}\right)^{n-1}$

$a_4 = 24300000 \left(\frac{7}{30}\right)^{4-1} = 308700$   $a_5 = 24300000 \left(\frac{7}{30}\right)^{5-1} = 72030$   $a_6 = 24300000 \left(\frac{7}{30}\right)^{6-1} = 16807$

$a_9 = 24300000 \left(\frac{7}{30}\right)^{9-1} = \frac{5764801}{27000} = 213.511148148$

Problem 11

	A	B	C	D	E	F	G	H
=								
1	a_1		88 ratio		31 diff		6	

AI a\_1

{ 88, 2728, 100936, 4340248 }

This is a recursive pattern The ratio between 2728 and 88 is 31 The ratio between 100936 and 2728 is 37  
The ratio between 4340248 and 100936 is 43

So a pattern for the change can be written as: multiply by 31  
Add 6 more to the multiplier than the last time to each term

a\_1 = 88      a\_5 = 4340248 (31 + (5-2)(6)) = 4340248 [49] = 212672152

a\_n = a\_{n-1} (31 + (n-2)(6))      a\_6 = 212672152 (31 + (6-2)(6)) = 212672152 + 55 = 11696968360

a\_7 = 11696968360 + (31 + (7-2)(6)) = 11696968360 + 61 = 713515069960

a\_1 = 88      a\_8 = 713515069960 + (31 + (8-2)(6)) = 713515069960 + 67 = 47805509687320

a\_n = a\_{n-1} (6 · n + 19)      a\_9 = 47805509687320 + (31 + (9-2)(6)) = 47805509687320 + 73 = 3489802207174360

This is a "fancier" version a\_1 = 88      a\_n = 88 + ∏\_{k=1}^{n-1} (31 + (k-1)(6))

88 + 186 · 2 + 2268	2728
2728 + 186 · 3 + 2268	5554
[ ]	

### Problem 12

	A	B	C	D	E	F	G	H
	=							
1	a_1	6144	differenc...	33792	ratio		13/2	

AI a\_1

{ 6144, 39936, 259584 }

This is a geometric pattern The ratio is 39936 divided by 6144 is  $\frac{13}{2}$

The ratio is 259584 divided by 39936 is  $\frac{13}{2}$

$a_1 = 6144$   $r = \frac{13}{2}$   $a_n = 6144 \left(\frac{13}{2}\right)^{n-1}$

$a_4 = 6144 \left(\frac{13}{2}\right)^{4-1} = 1687296$   $a_5 = 6144 \left(\frac{13}{2}\right)^{5-1} = 10967424$   $a_6 = 6144 \left(\frac{13}{2}\right)^{6-1} = 71288256$

$a_{12} = 6144 \left(\frac{13}{2}\right)^{12-1} = 5376481182111$

### Problem 13

Writing a sequence from two of its terms  
(non sequential)

Step 1) What type of sequence is given?  
When given arithmetic sequence terms

Step 2) Write the definition of each term using  $a_1$  and  $d$

Step 3) Solve the resulting linear system

Step 4) Write the arithmetic sequence using  $a_1$  and  $d$

Step 5) Complete the missing terms in the sequence to check to see that rule actually works for each term

	A	B
	=	
1	given_term1	-
2	term_in_seq1	
3	given_term2	
4	term_in_seq2	

AI given\_term1

So we know  $a_{13} = -960$  and  $a_{17} = 288$   
and we also know that this is an arithmetic sequence

so all terms must follow  $a_n = a_1 + (n-1)d$ ,  
including  $a_{13}$  and  $a_{17}$

$$\text{so } a_{13} = a_1 + (13-1)d \text{ or } -960 = a_1 + 12d$$

$$\text{so } a_{17} = a_1 + (17-1)d \text{ or } 288 = a_1 + 16d$$

This system can be solved a variety of ways, but basically you can subtract the higher sequence term and lower sequence term and it yields  $d$  and  $a_1$

	A	B	C
=			
1	a_5	-960	
2	a_15	288	
3			
4			
5			
6			
7			
8			
9			
10			
11			
A1 a_5			

$$a_{17} - a_{13} \text{ implies } 288 - (-960) = 1248$$

$$a_{17} - a_{13} \text{ implies } (a_1 + 16d) - (a_1 + 12d) = a_1 + 16d - a_1 - 12d = 4d$$

$$\text{This allows us to find "d" } \quad 1248 = 4d$$

$$1248 / 4 = 4d / 4$$

$$312 = d$$

We can now use either  $-960 = a_1 + 12d$  or  $288 = a_1 + 16d$  to find  $a_1$

$$-960 = a_1 + 12(312) \text{ leads to } -960 = a_1 + 3744 \text{ or } a_1 = -960 - 3744 = -4704$$

$$288 = a_1 + 16(312) \text{ leads to } 288 = a_1 + 4992 \text{ or } a_1 = 288 - 4992 = -4704$$

**so our arithmetic sequence is  $a_n = -4704 + (n-1)(312)$**

**and our finite sequence is**

$$\{-4704, -4392, -4080, -3768, -3456, -3144, -2832, -2520, -2208, -1896, -1584, -1272, -960\}$$

Problem 14

Writing a sequence from two of its terms (non sequential)

Step 1) What type of sequence is given?

When given geometric sequence terms

Step 2) Write the definition of each term using  $a_1$  and  $r$

Step 3) Solve the resulting proportion

(I suggest putting higher sequence term (not value) on top)

(this will require radical operations)

Step 4) Write the geometric sequence using  $a_1$  and  $r$

Step 5) Complete the missing terms in the sequence to check to see that rule actually works for each term

	A	B	C
=			
1	given_term1	279936/...	
2	term_in_seq1	6	
3	given_term2	1296/24...	
4	term_in_seq2	9	
5			
6			
7			
8			
9			
10			
11			

A1 given\_term1

So we know  $a_2 = \frac{279936}{823543}$  and  $a_7 = \frac{1296}{2401}$  and we also know that this is an geometric sequence so all terms must follow  $a_n = a_1(r)^{n-1}$ , including  $a_1$  and  $a_7$

so  $a_2 = a_1 r^{(6-1)}$  or  $\frac{279936}{823543} = a_1 \cdot r^5$

so  $a_7 = a_1 r^{(9-1)}$  or  $\frac{1296}{2401} = a_1 \cdot r^8$

This system can be solved a variety of ways, but basically you can divide the higher sequence term and lower sequence term then apply necessary radical and it yields  $r$  and  $a_1$

	A	B	C
=			
1	a_2	279936/...	
2	a_7	1296/24...	
3			
4			
5			
6			
7			
8			
9			
10			
11			

A1 a\_2

$$a_9/a_6 \text{ implies } \frac{1296}{2401} / \frac{279936}{823543} = \frac{343}{216}$$

$$a_9/a_6 \text{ implies } a_1 \cdot r^8 / a_1 \cdot r^5 = r^3$$

This allows us to find "r"  $r^3 = \frac{343}{216}$  which leads to  $\sqrt[3]{r^3} = \sqrt[3]{\frac{343}{216}}$

$$r = \frac{7}{6}$$

I would use the smaller sequence term to use  $\frac{279936}{823543} = a_1 \cdot r^5$  to find  $a_1$

$$\frac{279936}{823543} = a_1 \left(\frac{7}{6}\right)^5 \text{ which leads to } \frac{279936}{823543} = \frac{16807}{7776} a_1$$

$$\text{which leads to } \frac{279936}{823543} \cdot \left(\frac{7776}{16807}\right) = \left(\frac{7776}{16807}\right) \left(\frac{16807}{7776}\right) \text{ or } a_1 = \frac{2176782336}{13841287201}$$

so our geometric sequence is  $a_n = \frac{2176782336}{13841287201} \left(\frac{7}{6}\right)^{(n-1)}$

and our finite sequence is

$$\left\{ \frac{2176782336}{13841287201}, \frac{362797056}{1977326743}, \frac{60466176}{282475249}, \frac{10077696}{40353607}, \frac{1679616}{5764801}, \frac{279936}{823543}, \frac{46656}{117649}, \frac{7776}{16807}, \frac{1296}{2401} \right\}$$

$$\frac{7}{6} \rightarrow 1.16666666667$$

$$1 \cdot a_1 \rightarrow 0.157267333911$$

□

Problem 15

A	seq_1
=	
1	105
2	126
3	147
4	168
5	189
6	210
7	231
AI	105

$105 + 126 + 147 + 168 + 189 + 210 + 231 + 252 + 273 + 294 + 315 + 336 + 357 + 378 + 399 + 420 + 441$

this is the sum of the following arithmetic sequence

$\{ 105, 126, 147, 168, 189, 210, 231, 252, 273, 294, 315, 336, 357, 378, 399, 420, 441 \}$

Method 1: count terms (this is n)  $n = 17$

add first and last terms

First term ( $a_1$ ) = 105    Last term ( $a_{17}$ ) = 441

Sum of first and last term  $105 + 441 = 546$

multiply sum of first and last terms by 1/2 the number of terms

$17$

$$\sum_{n=1}^{17} 105 + (n-1)(21) = 4641 \quad \text{This is how Riemann would have applied}$$

Problem 16

A	seq_1
=	
1	64/729
2	128/2187
3	256/6561
4	512/196...
5	1024/59...
6	2048/17...
AI	64/729

$\frac{64}{729} + \frac{128}{2187} + \frac{256}{6561} + \frac{512}{19683} + \frac{1024}{59049} + \frac{2048}{177147} + \frac{4096}{531441}$

this is the sum of the following geometric sequence

$\left\{ \frac{64}{729}, \frac{128}{2187}, \frac{256}{6561}, \frac{512}{19683}, \frac{1024}{59049}, \frac{2048}{177147}, \frac{4096}{531441} \right\}$

Method 1: Count terms (this is n)  $n = 7$

Determine  $a_1$  and  $r$  First term ( $a_1$ ) =  $\frac{64}{729}$      $r = \frac{2}{3}$

Use  $S_n = a_1 \cdot \frac{1-(r)^n}{1-r}$

$S_7 = \frac{64}{729} \cdot (1 - (\frac{2}{3})^7) / (1 - \frac{2}{3}) = a_1 \cdot \frac{1-r_1^{n-1}}{1-r_1} = \frac{131776}{531441}$

$$\sum_{n=1}^7 \frac{64}{729} \left(\frac{2}{3}\right)^{(n-1)} = \frac{131776}{531441} \quad \text{This is how Riemann would have applied}$$

1.0p    0.247959792338

Problem 17

	A missed	B raw	C percent	D	E	F	G	H
=		=140-mis	=raw/(1.4)					
1	0	140	100.					
2	0.5	139.5	99.6428...					
3	1.	139.	99.2857...					
4	1.5	138.5	98.9285...					
5	2.	138.	98.5714...					
6	2.5	137.5	98.2142...					
7	3.	137.	97.8571...					
8	3.5	136.5	97.5					
9	4.	136.	97.1428...					
10	4.5	135.5	96.7857...					
11	5.	135.	96.4285...					
<div style="border: 1px solid black; padding: 2px;"> <span style="float: left;">A1</span> 0         </div>								