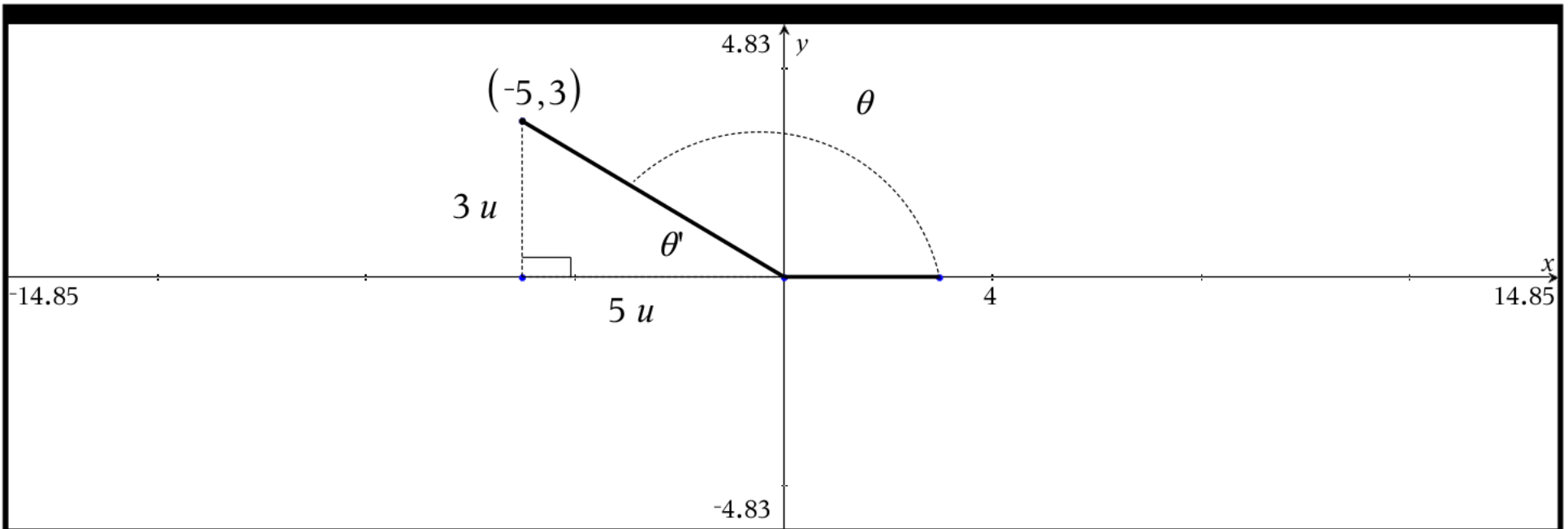


Quadrant 2



$$x = -5 \quad y = 3 \quad r^2 = x^2 + y^2 = (-5)^2 + (3)^2 = 25 + 9 = 34 \quad \text{implies } r = \sqrt{34}$$

$$\theta \approx 149.036^\circ \approx 2.60117 \text{ radians} \quad \theta' = \text{reference angle} \approx 30.9638^\circ \approx 0.54042 \text{ radians}$$

$$\sin \theta = 3 / \sqrt{34} = \frac{3 \cdot \sqrt{34}}{34}$$

$$\cos \theta = -5 / \sqrt{34} = \frac{-5 \cdot \sqrt{34}}{34}$$

$$\tan \theta = 3 / -5 = \frac{-3}{5}$$

$$\csc \theta = \sqrt{34} / 3 = \frac{\sqrt{34}}{3}$$

$$\sec \theta = \sqrt{34} / -5 = \frac{-\sqrt{34}}{5}$$

$$\cot \theta = -5 / 3 = \frac{-5}{3}$$

NEVER calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = 3/\sqrt{34} = \frac{3 \cdot \sqrt{34}}{34}$$

$$\theta' = \sin^{-1}(3/\sqrt{34}) \approx 30.9638^\circ$$

Since this point $(-5, 3)$ is in quadrant 2 $\theta = 180^\circ - \sin^{-1}(3/\sqrt{34}) \approx 149.036^\circ$

$$\cos \theta' = 5/\sqrt{34} = \frac{5 \cdot \sqrt{34}}{34}$$

$$\theta' = \cos^{-1}(5/\sqrt{34}) \approx 30.9638^\circ$$

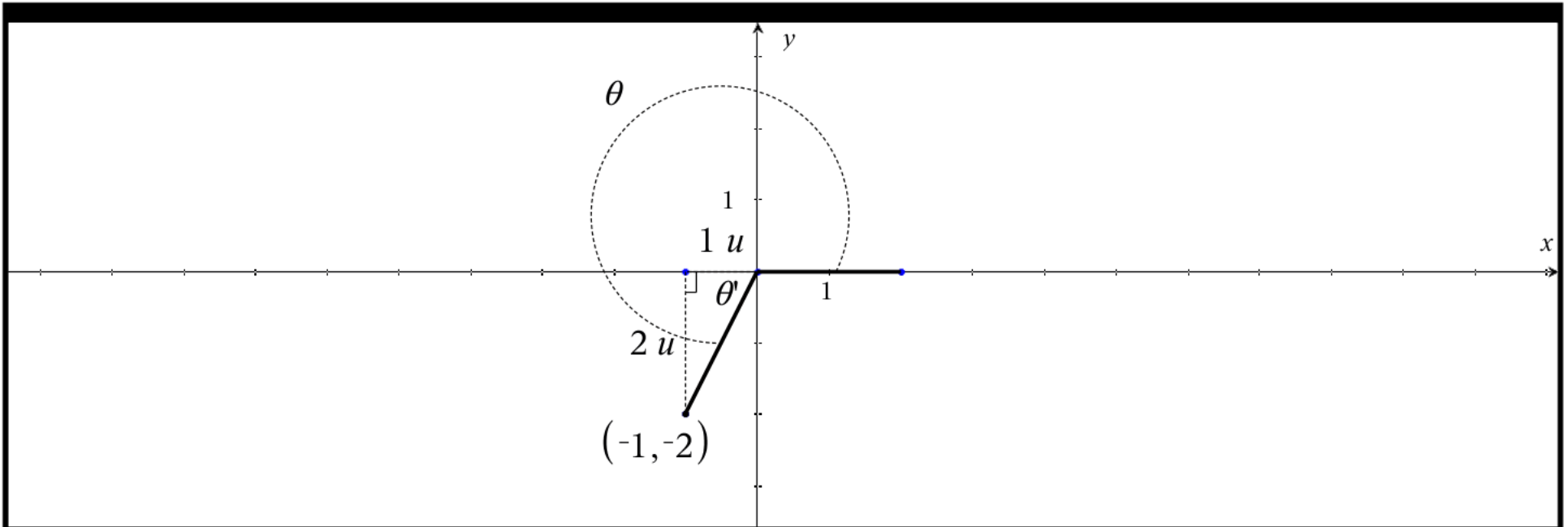
Since this point $(-5, 3)$ is in quadrant 2 $\theta = 180^\circ - \cos^{-1}(5/\sqrt{34}) \approx 149.036^\circ$

$$\tan \theta' = 3/5 = \frac{3}{5}$$

$$\theta' = \tan^{-1}(3/5) \approx 30.9638^\circ$$

Since this point $(-5, 3)$ is in quadrant 2 $\theta = 180^\circ - \tan^{-1}(3/5) \approx 149.036^\circ$

Quadrant 3



$$x = -1 \quad y = -2 \quad r^2 = x^2 + y^2 = (-1)^2 + (-2)^2 = 1 + 4 = 5 \text{ implies } r = \sqrt{5} = \sqrt{5}$$

$$\theta \approx 243.435^\circ \approx 4.24874 \text{ radians} \quad \theta' = \text{reference angle} \approx 63.4349^\circ \approx 1.10715 \text{ radians}$$

$$\sin \theta = -2/\sqrt{5} = \frac{-2 \cdot \sqrt{5}}{5}$$

$$\cos \theta = -1/\sqrt{5} = \frac{-\sqrt{5}}{5}$$

$$\tan \theta = -2/-1 = 2$$

$$\csc \theta = \sqrt{5} / -2 = \frac{-\sqrt{5}}{2}$$

$$\sec \theta = \sqrt{5} / -1 = -\sqrt{5}$$

$$\cot \theta = -1/-2 = \frac{1}{2}$$

NEVER calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = 2/\sqrt{5} = \frac{2 \cdot \sqrt{5}}{5}$$

$$\theta' = \sin^{-1}(2/\sqrt{5}) \approx 63.4349^\circ$$

Since this point $(-1, -2)$ is in quadrant 3 $\theta = 180^\circ + \sin^{-1}(2/\sqrt{5}) \approx 243.435^\circ$

$$\cos \theta' = 1/\sqrt{5} = \frac{\sqrt{5}}{5}$$

$$\theta' = \cos^{-1}(1/\sqrt{5}) \approx 63.4349^\circ$$

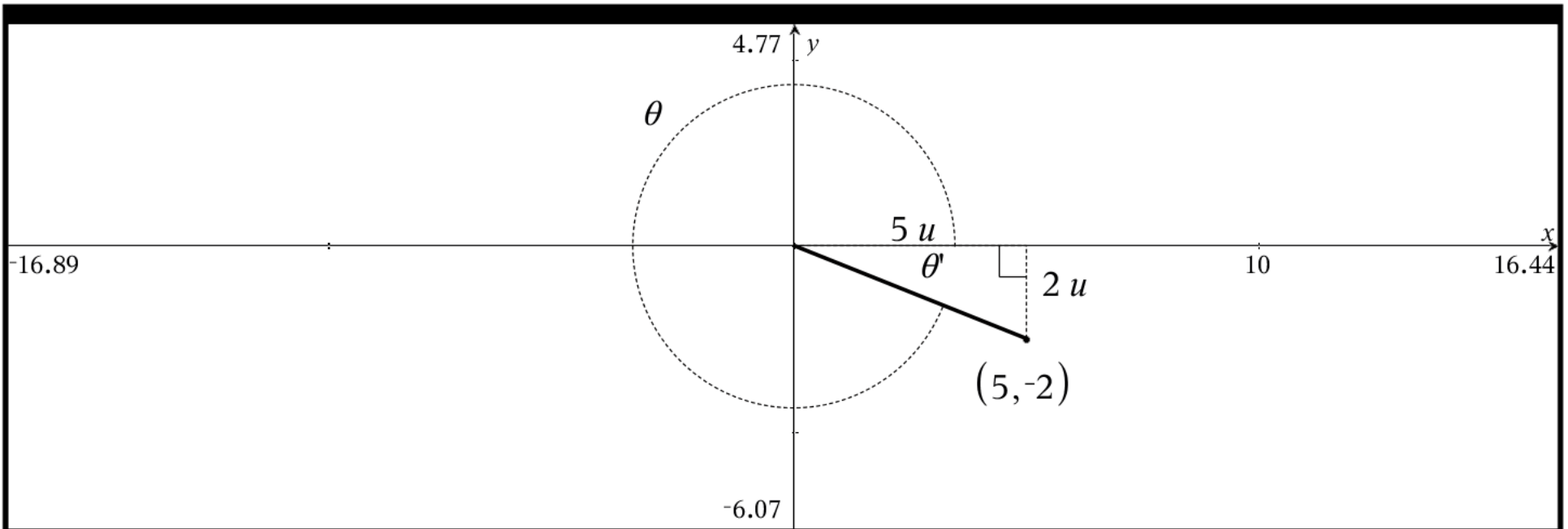
Since this point $(-1, -2)$ is in quadrant 3 $\theta = 180^\circ + \cos^{-1}(1/\sqrt{5}) \approx 243.435^\circ$

$$\tan \theta' = 2/1 = 2$$

$$\theta' = \tan^{-1}(2/1) \approx 63.4349^\circ$$

Since this point $(-1, -2)$ is in quadrant 3 $\theta = 180^\circ + \tan^{-1}(2/1) \approx 243.435^\circ$

Quadrant 4



$$x = 5 \quad y = -2 \quad r^2 = x^2 + y^2 = (5)^2 + (-2)^2 = 25 + 4 = 29 \quad \text{implies } r = \sqrt{29}$$

$$\theta \approx 338.199^\circ \approx 5.90268 \text{ radians} \quad \theta' = \text{reference angle} \approx 21.8014^\circ \approx 0.380506 \text{ radians}$$

$$\sin \theta = -2/\sqrt{29} = \frac{-2 \cdot \sqrt{29}}{29}$$

$$\cos \theta = 5/\sqrt{29} = \frac{5 \cdot \sqrt{29}}{29}$$

$$\tan \theta = -2/5 = \frac{-2}{5}$$

$$\csc \theta = \sqrt{29} / -2 = \frac{-\sqrt{29}}{2}$$

$$\sec \theta = \sqrt{29} / 5 = \frac{\sqrt{29}}{5}$$

$$\cot \theta = 5 / -2 = \frac{-5}{2}$$

NEVER calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = 2/\sqrt{29} = \frac{2 \cdot \sqrt{29}}{29}$$

$$\theta' = \sin^{-1}(2/\sqrt{29}) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \sin^{-1}(2/\sqrt{29}) \approx 338.199^\circ$$

$$\cos \theta' = 5/\sqrt{29} = \frac{5 \cdot \sqrt{29}}{29}$$

$$\theta' = \cos^{-1}(5/\sqrt{29}) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \cos^{-1}(5/\sqrt{29}) \approx 338.199^\circ$$

$$\tan \theta' = 2/5 = \frac{2}{5}$$

$$\theta' = \tan^{-1}(2/5) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \tan^{-1}(2/5) \approx 338.199^\circ$$