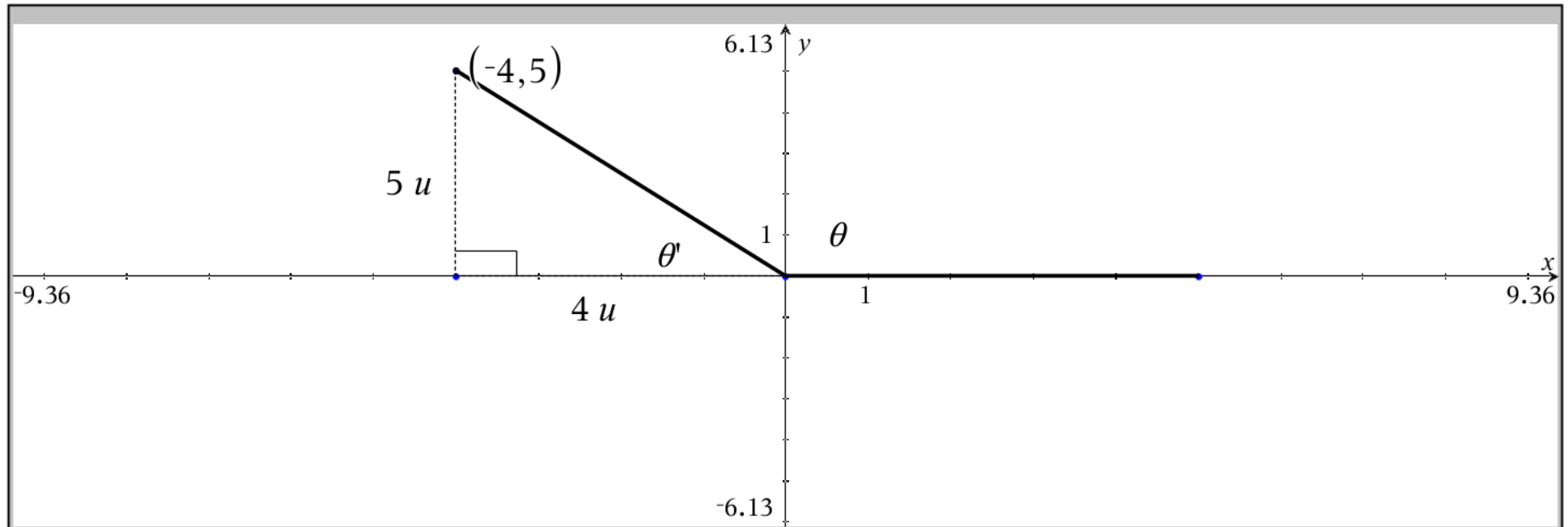


Quadrant 2



$$x = -4 \quad y = 5 \quad r^2 = x^2 + y^2 = (-4)^2 + (5)^2 = 16 + 25 = 41 \quad \text{implies } r = \sqrt{41} = \sqrt{41}$$

$$\theta \approx 128.66^\circ \approx 2.24554 \text{ radians} \quad \theta' = \text{reference angle} \approx 51.3402^\circ \approx 0.896055 \text{ radians}$$

$$\sin \theta = 5 / \sqrt{41} = \frac{5 \cdot \sqrt{41}}{41}$$

$$\cos \theta = -4 / \sqrt{41} = \frac{-4 \cdot \sqrt{41}}{41}$$

$$\tan \theta = 5 / -4 = \frac{-5}{4}$$

$$\csc \theta = \sqrt{41} / 5 = \frac{\sqrt{41}}{5}$$

$$\sec \theta = \sqrt{41} / -4 = \frac{-\sqrt{41}}{4}$$

$$\cot \theta = -4 / 5 = \frac{-4}{5}$$

SO..... never calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = \frac{5}{\sqrt{41}} = \frac{5 \cdot \sqrt{41}}{41} \qquad \theta' = \sin^{-1} \left(\frac{5}{\sqrt{41}} \right) \approx 51.3402^\circ$$

Since this point $(-4, 5)$ is in quadrant 2 $\theta = 180^\circ - \sin^{-1} \left(\frac{5}{\sqrt{41}} \right) \approx 128.66^\circ$

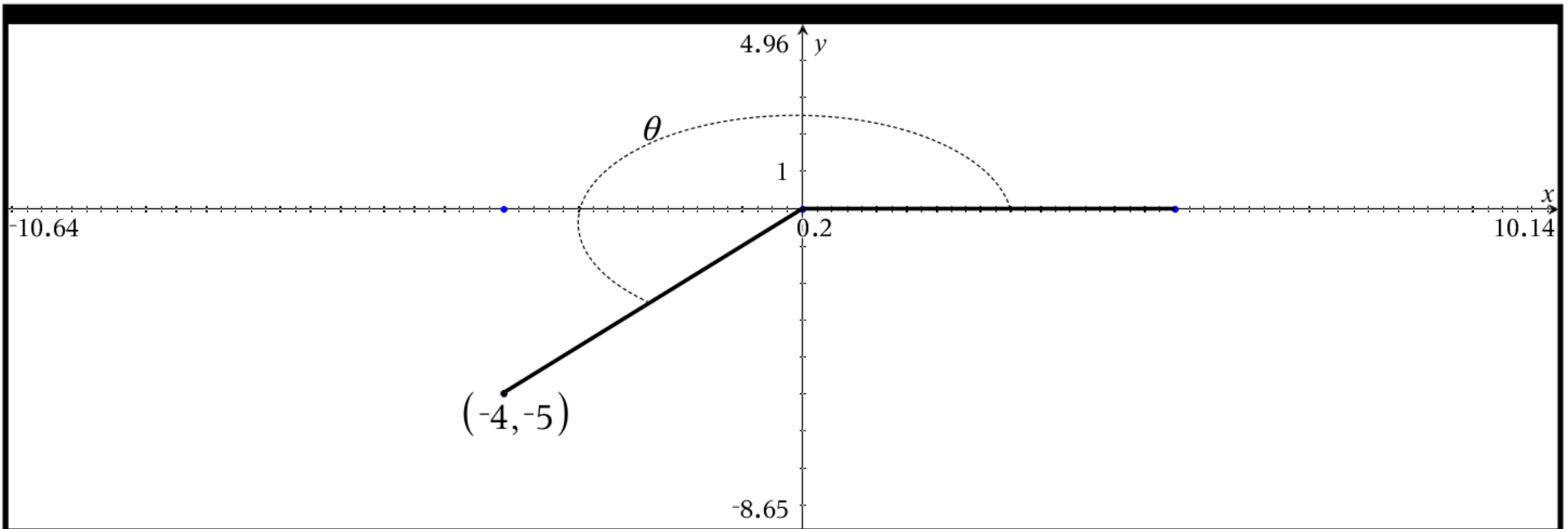
$$\cos \theta' = \frac{4}{\sqrt{41}} = \frac{4 \cdot \sqrt{41}}{41} \qquad \theta' = \cos^{-1} \left(\frac{4}{\sqrt{41}} \right) \approx 51.3402^\circ$$

Since this point $(-4, 5)$ is in quadrant 2 $\theta = 180^\circ - \cos^{-1} \left(\frac{4}{\sqrt{41}} \right) \approx 128.66^\circ$

$$\tan \theta' = \frac{5}{4} \qquad \theta' = \tan^{-1} \left(\frac{5}{4} \right) \approx 51.3402^\circ$$

Since this point $(-4, 5)$ is in quadrant 2 $\theta = 180^\circ - \tan^{-1} \left(\frac{5}{4} \right) \approx 128.66^\circ$

Quadrant 3



$$x = -4 \quad y = -5 \quad r^2 = x^2 + y^2 = (-4)^2 + (-5)^2 = 16 + 25 = 41 \quad \text{implies } r = \sqrt{41} = \sqrt{41}$$

$$\theta \approx 231.34^\circ \approx 4.03765 \text{ radians} \quad \theta' = \text{reference angle} \approx 51.3402^\circ \approx 0.896055 \text{ radians}$$

$$\sin \theta = -5 / \sqrt{41} = \frac{-5 \cdot \sqrt{41}}{41}$$

$$\cos \theta = -4 / \sqrt{41} = \frac{-4 \cdot \sqrt{41}}{41}$$

$$\tan \theta = -5 / -4 = \frac{5}{4}$$

$$\csc \theta = \sqrt{41} / -5 = \frac{-\sqrt{41}}{5}$$

$$\sec \theta = \sqrt{41} / -4 = \frac{-\sqrt{41}}{4}$$

$$\cot \theta = -4 / -5 = \frac{4}{5}$$

SO..... never calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = \frac{5}{\sqrt{41}} = \frac{5 \cdot \sqrt{41}}{41}$$

$$\theta' = \sin^{-1} \left(\frac{5}{\sqrt{41}} \right) \approx 51.3402^\circ$$

Since this point $(-4, -5)$ is in quadrant 3

$$\theta = 180^\circ + \sin^{-1} \left(\frac{5}{\sqrt{41}} \right) \approx 231.34^\circ$$

$$\cos \theta' = \frac{4}{\sqrt{41}} = \frac{4 \cdot \sqrt{41}}{41}$$

$$\theta' = \cos^{-1} \left(\frac{4}{\sqrt{41}} \right) \approx 51.3402^\circ$$

Since this point $(-4, -5)$ is in quadrant 3

$$\theta = 180^\circ + \cos^{-1} \left(\frac{4}{\sqrt{41}} \right) \approx 231.34^\circ$$

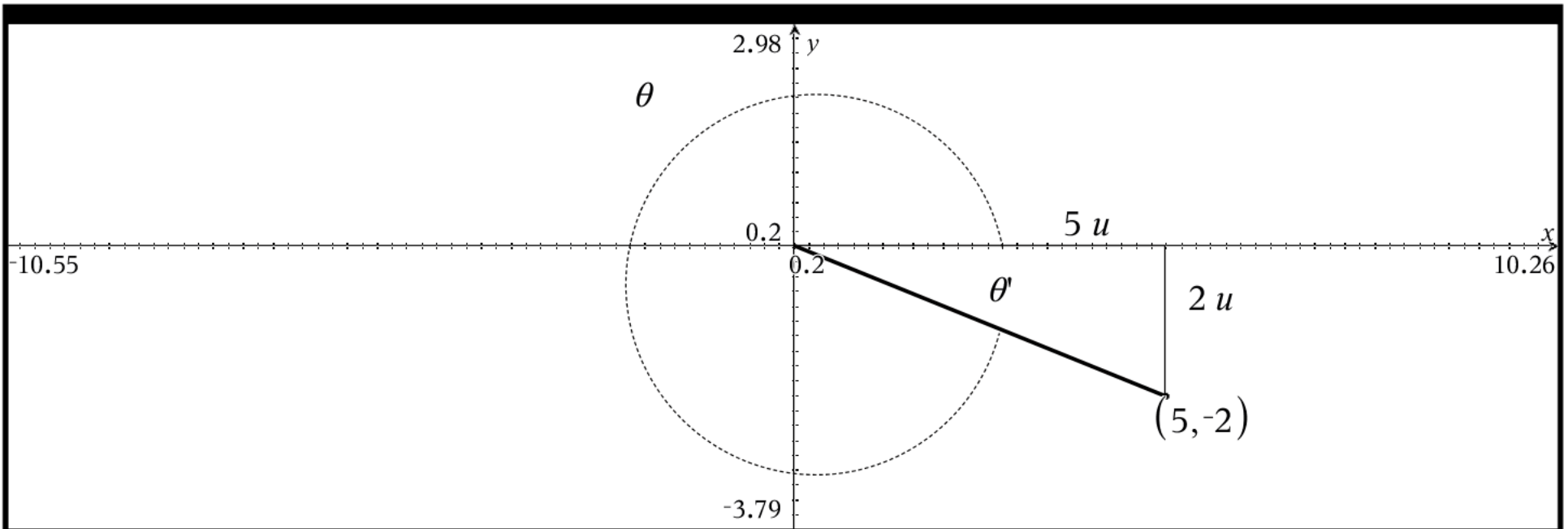
$$\tan \theta' = \frac{5}{4} = \frac{5}{4}$$

$$\theta' = \tan^{-1} \left(\frac{5}{4} \right) \approx 51.3402^\circ$$

Since this point $(-4, -5)$ is in quadrant 3

$$\theta = 180^\circ + \tan^{-1} \left(\frac{5}{4} \right) \approx 231.34^\circ$$

Problem 3



$$x = 5 \quad y = -2 \quad r^2 = x^2 + y^2 = (5)^2 + (-2)^2 = 25 + 4 = 29 \quad \text{implies } r = \sqrt{29}$$

$$\theta \approx 338.199^\circ \approx 5.90268 \text{ radians} \quad \theta' = \text{reference angle} \approx 21.8014^\circ \approx 0.380506 \text{ radians}$$

$$\sin \theta = -2/\sqrt{29} = \frac{-2 \cdot \sqrt{29}}{29}$$

$$\cos \theta = 5/\sqrt{29} = \frac{5 \cdot \sqrt{29}}{29}$$

$$\tan \theta = -2/5 = \frac{-2}{5}$$

$$\csc \theta = \sqrt{29} / -2 = \frac{-\sqrt{29}}{2}$$

$$\sec \theta = \sqrt{29} / 5 = \frac{\sqrt{29}}{5}$$

$$\cot \theta = 5 / -2 = \frac{-5}{2}$$

SO..... never calculate the reference angle in any quadrant BUT quadrant 1,
THEN reference into quadrant that the point lies in

$$\sin \theta' = 2/\sqrt{29} = \frac{2 \cdot \sqrt{29}}{29}$$

$$\theta' = \sin^{-1}(2/\sqrt{29}) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \sin^{-1}(2/\sqrt{29}) \approx 338.199^\circ$$

$$\cos \theta' = 5/\sqrt{29} = \frac{5 \cdot \sqrt{29}}{29}$$

$$\theta' = \cos^{-1}(5/\sqrt{29}) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \cos^{-1}(5/\sqrt{29}) \approx 338.199^\circ$$

$$\tan \theta' = 2/5 = \frac{2}{5}$$

$$\theta' = \tan^{-1}(2/5) \approx 21.8014^\circ$$

Since this point (5, -2) is in quadrant 4

$$\theta = 360^\circ - \tan^{-1}(2/5) \approx 338.199^\circ$$