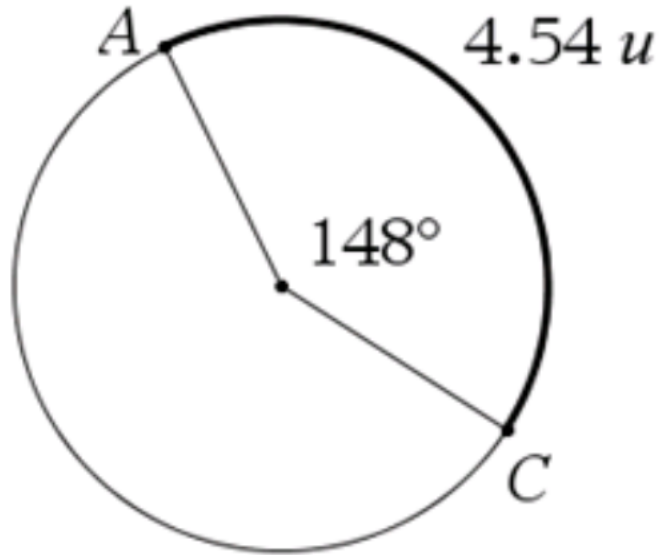


Problem 1



Determine the radius of the circle

$$s = \theta r$$

We know $s = 4.54$ units

we know angle in degrees is 148°

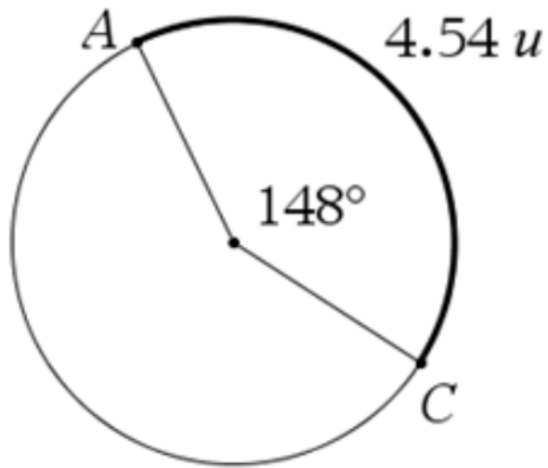
Step 1) Find θ

$$\theta = 148^\circ \cdot \frac{\pi \text{ radians}}{180^\circ}$$

$$= \frac{148}{180} \pi \text{ radians} = \frac{37}{45} \pi \text{ radians}$$

Step 2) Solve for r

$$4.54 = \left(\frac{148}{180} \pi \right) r$$



Determine the radius of the circle

$$s = \theta r$$

$$s = 4.54 \text{ units}$$

angle in degrees is 148°

$$\theta = \frac{37}{45} \pi \text{ radians}$$

Use $s = \theta r$ replace s and θ and solve for r

Step 2) Solve for r

$$4.54 = \left(\frac{148}{180} \pi \right) r$$

$$\frac{4.54}{1} = \frac{148\pi r}{180}$$

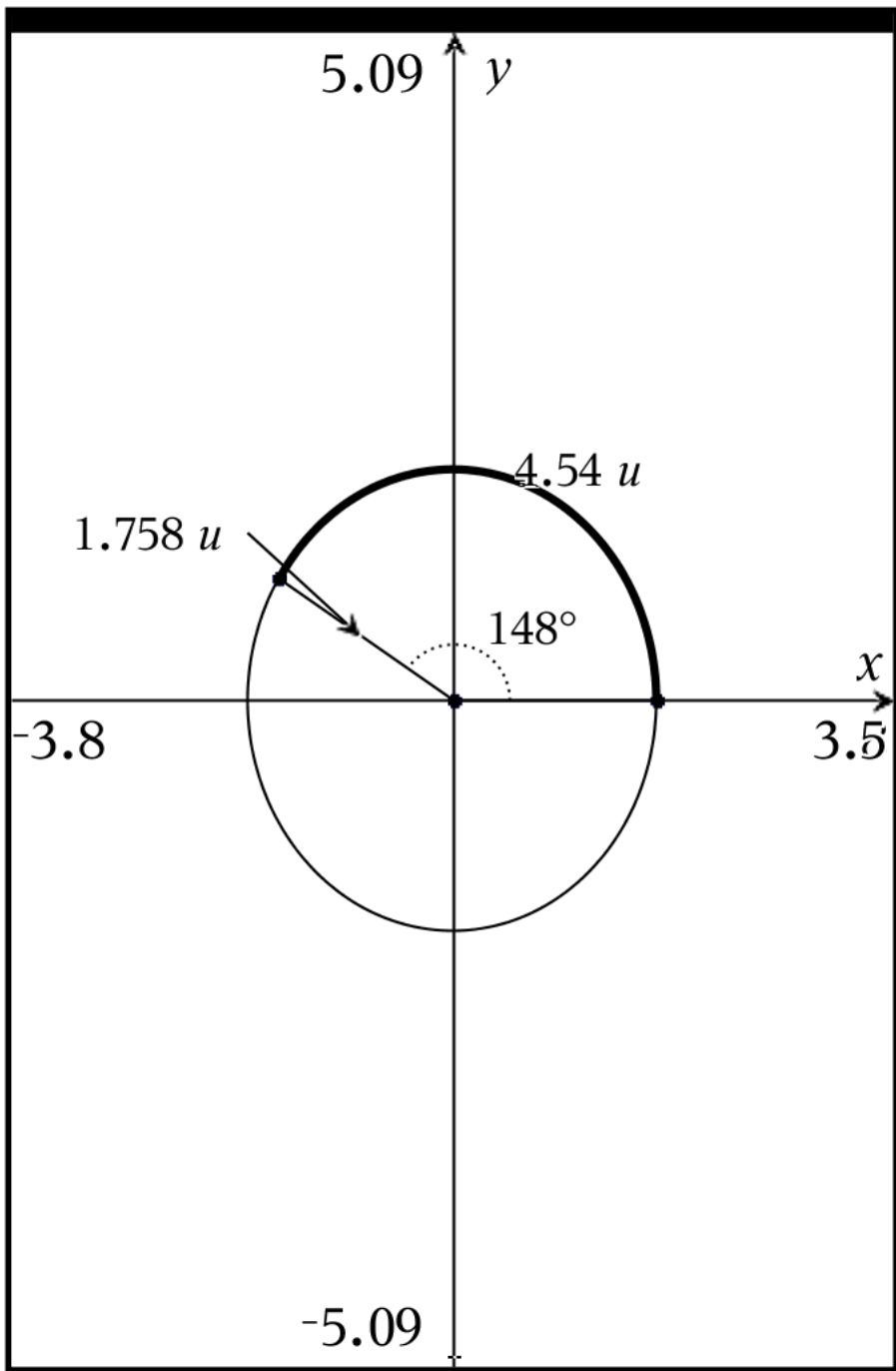
$$4.54 \cdot 180 = 148\pi r$$

$$817.2 = 148\pi r$$

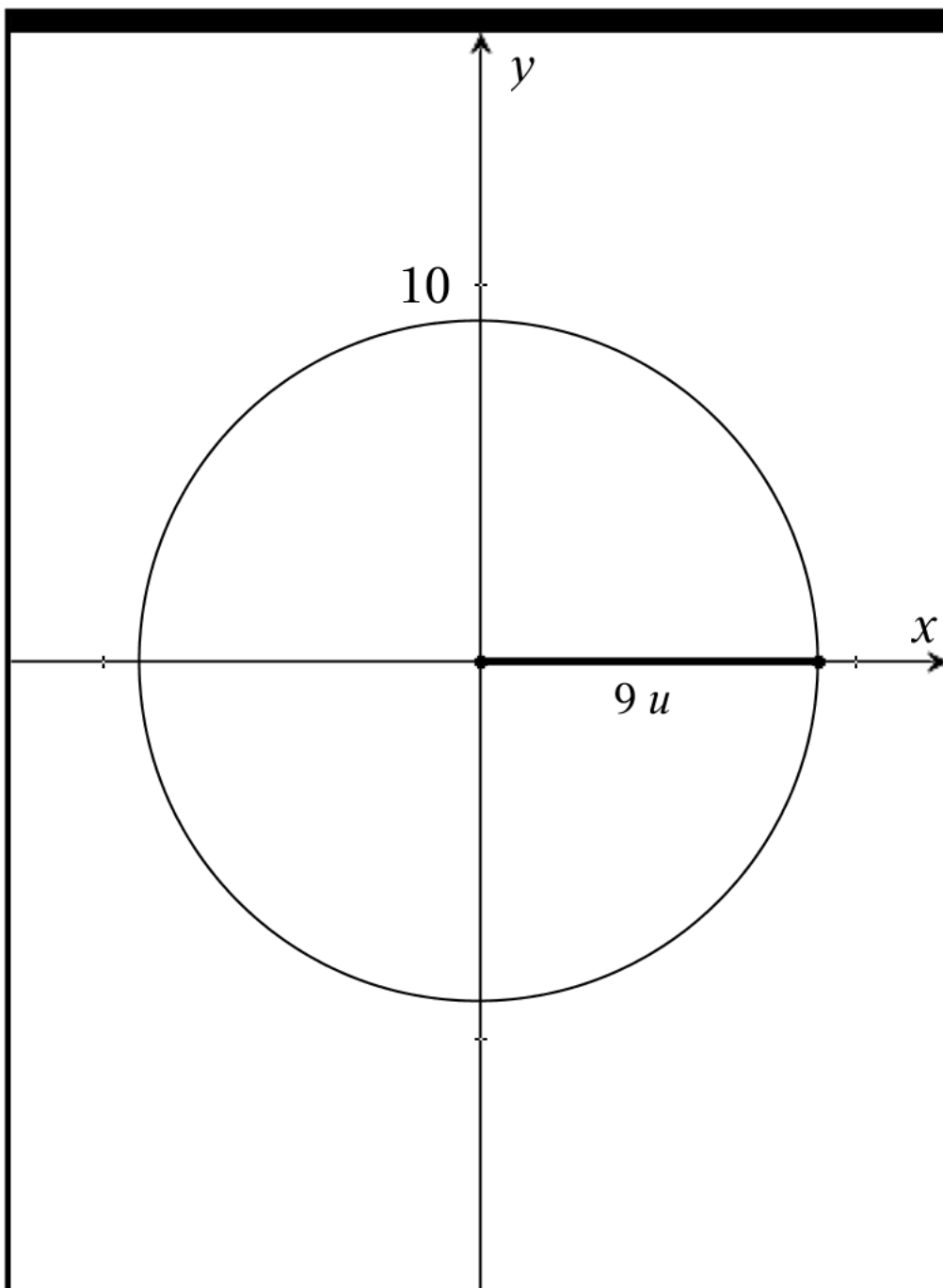
$$\frac{817.2}{148\pi} = \frac{148\pi r}{148\pi}$$

$$r = \frac{817.2}{148\pi} = \frac{8172}{1480\pi} = \frac{2043}{370 \cdot \pi}$$

$$r \approx 1.758 \text{ units}$$



This drawing was created with a computer and it checks that the radius is $1.75759 \approx 1.758$



Drum with a diameter of 18 meters is making 5.6 revolutions per minute

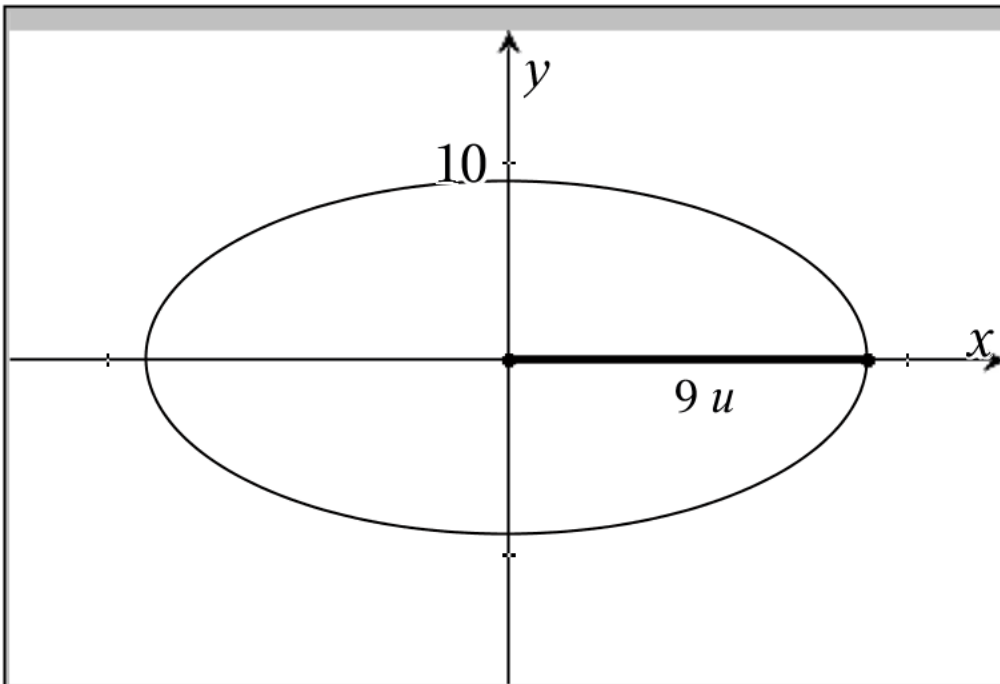
5.6 revolutions per min

$$\begin{aligned} \text{Angular speed} &= \frac{5.6 \text{ rev.}}{\text{min.}} \cdot \frac{360^\circ}{\text{rev}} \\ &= \frac{2016^\circ}{\text{min}} \end{aligned}$$

$$\begin{aligned} \text{Angular speed} &= \frac{5.6 \text{ rev.}}{\text{min.}} \cdot \frac{2\pi}{\text{rev}} \\ &= \frac{11.2\pi \text{ radians}}{\text{min}} \end{aligned}$$

Note Linear Speed = (Angular speed)(radius)

$$\begin{aligned} &= \frac{11.2\pi \text{ radians}}{\text{min}} \cdot \frac{9\text{m.}}{\text{radian}} \\ &= \frac{100.8\pi \text{ m}}{\text{min}} \end{aligned}$$



$$\text{Angular speed} = \frac{5.6 \text{ rev.}}{\text{min.}} \cdot \frac{2\pi}{\text{rev}}$$

$$= \frac{11.2\pi \text{ radians}}{\text{min}}$$

$$\theta = 11.2 \cdot \pi \text{ radians} \quad r = \frac{18}{2} = 9 \text{ meters}$$

Drum with a diameter of 18 meters is making 5.6 revolutions per minute

$$\text{Linear Speed} = \frac{\theta r}{t} = \frac{11.2 \cdot \pi \cdot 9 \text{ m.}}{1 \text{ min.}}$$

$$= \frac{100.8 \cdot \pi \text{ m.}}{1 \text{ min}}$$

$$\approx 316.673 \frac{\text{m.}}{\text{min.}}$$

Now convert meters/min to meters/sec

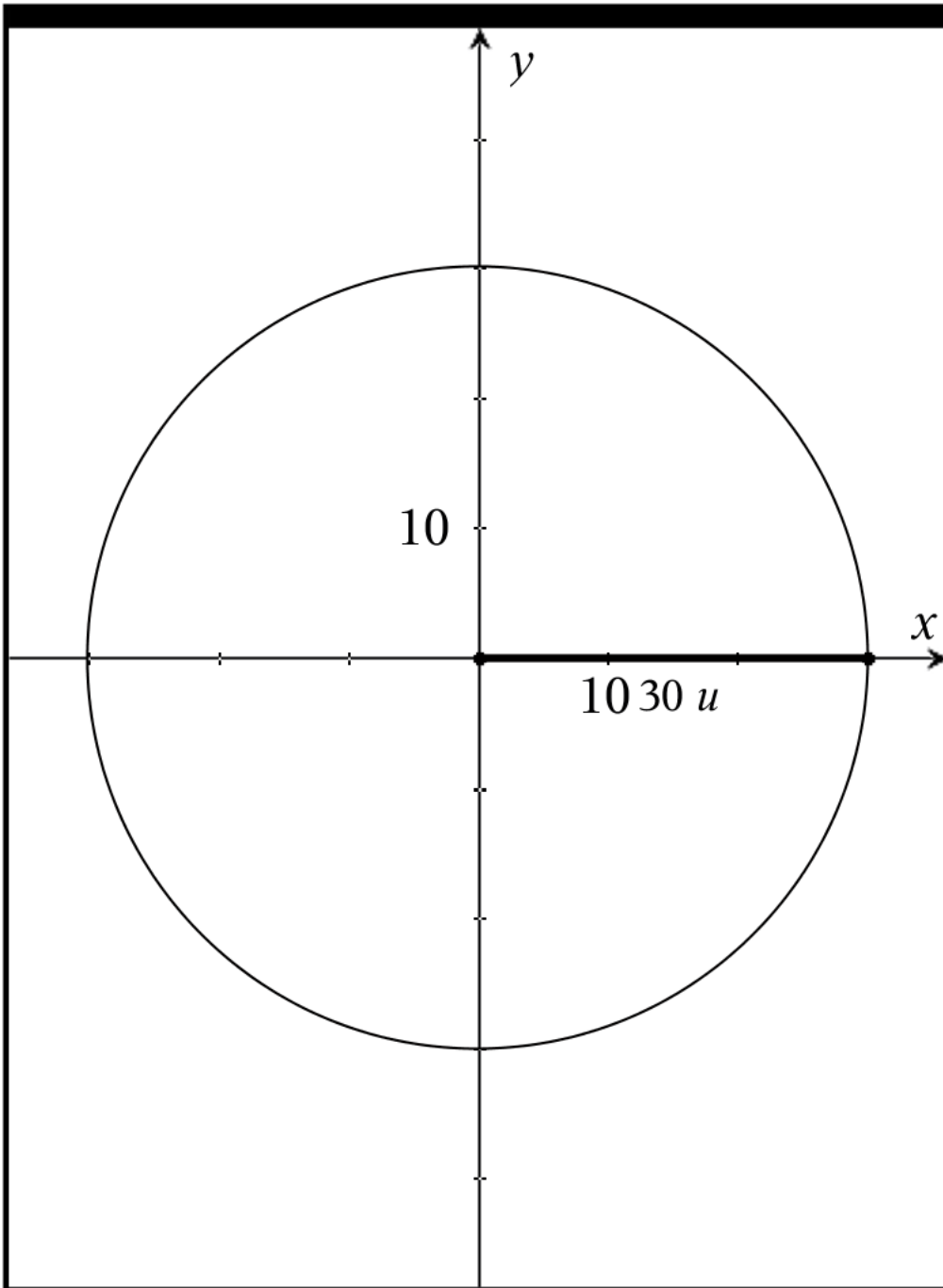
$$\text{Linear Speed} = \frac{100.8 \cdot \pi \text{ m.}}{1 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}}$$

$$= \frac{100.8\pi \text{ m.}}{60 \text{ sec}} = \frac{1.68\pi \text{ m.}}{\text{sec}}$$

$$= \frac{42\pi}{25} \frac{\text{m.}}{\text{sec.}}$$

$$\approx 5.278 \frac{\text{m}}{\text{sec}}$$

Problem 3



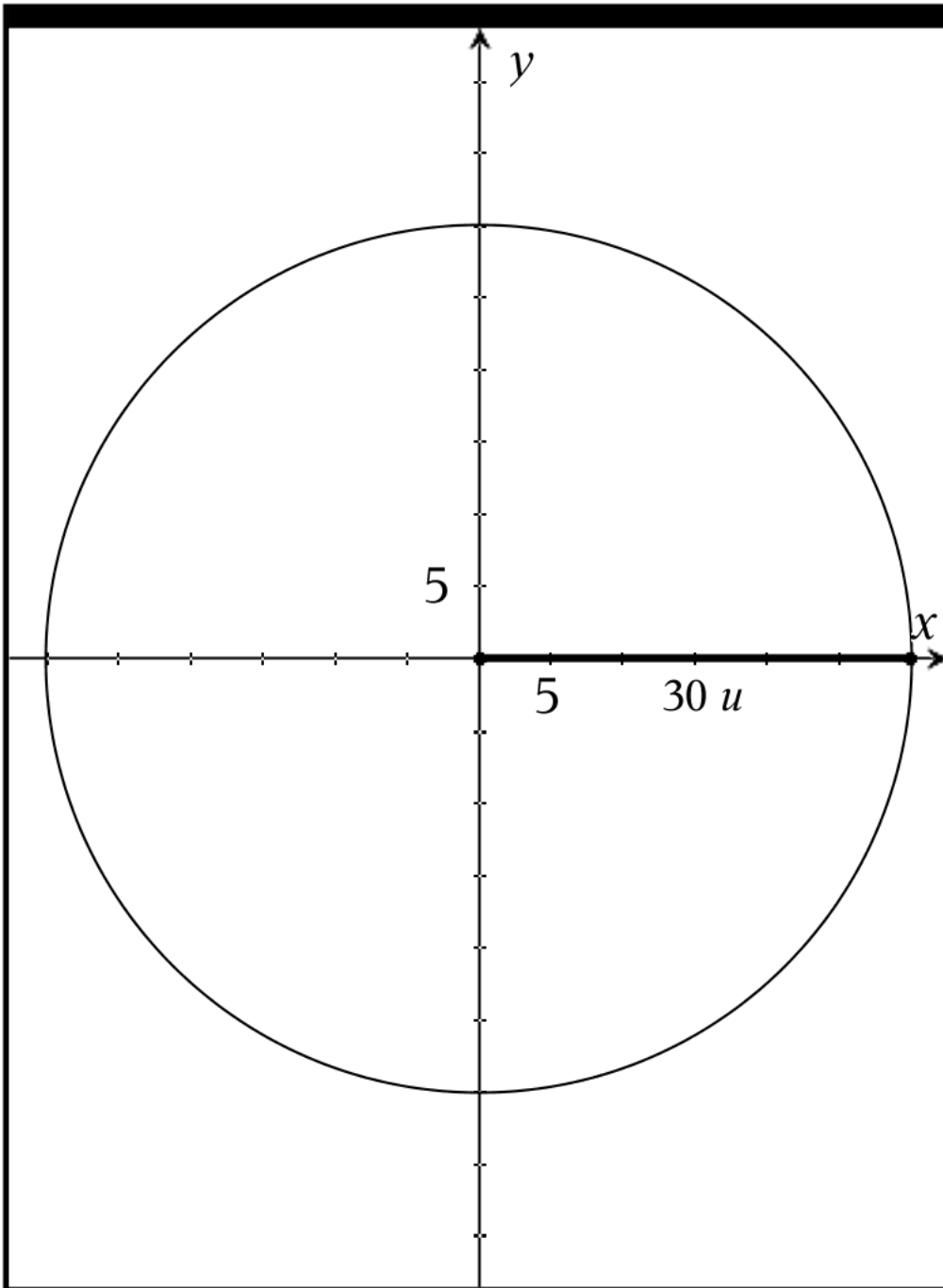
tire with a radius of 30 meters is making 3.5 revolutions per 25 seconds

3.5 revolutions per 25 seconds

$$\frac{3.5}{25} = 0.14 \text{ revolution per second}$$

$$\begin{aligned} \text{Angular speed} &= \frac{0.14 \text{ rev.}}{\text{sec.}} \cdot \frac{360^\circ}{\text{rev}} \\ &= \frac{50.4^\circ}{\text{sec}} \end{aligned}$$

$$\begin{aligned} \text{Angular speed} &= \frac{0.14 \text{ rev.}}{\text{sec.}} \cdot \frac{2\pi}{\text{rev}} \\ &= \frac{0.28\pi \text{ radians}}{\text{sec}} \end{aligned}$$



tire with a radius of 30 inches is making 3.5 revolutions per 25 seconds

$$\begin{aligned} \text{Angular speed} &= \frac{0.14 \text{ rev.}}{\text{sec.}} \cdot \frac{2\pi}{\text{rev}} \\ &= \underline{0.28\pi \text{ radians}} \\ &\quad \text{sec} \\ &\approx 0.88 \frac{\text{radians}}{\text{sec}} \end{aligned}$$

Now convert radians/sec to radians/min

$$\begin{aligned} \text{Angular Speed} &= \frac{0.28 \cdot \pi \text{ radians.}}{1 \text{ sec}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} \\ &= \underline{16.8\pi \text{ radians}} \quad 0.28 \cdot 60 \blacktriangleright 16.8 \\ &\quad \text{1min} \\ &\approx 52.779 \frac{\text{radians}}{\text{min}} \end{aligned}$$